ISO/IEC DTR 13211–3:2006
Definite clause grammar rules

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Introduction

This technical recommendation (TR) is an optional part of the International Standard for Prolog, ISO/IEC 13211. Prolog manufacturers wishing to implement Definite Clause Grammar rules in a portable way shall do so in compliance with this technical recommendation.

Grammar rules provide convenient and simple functionality for parsing and processing text in a variety of languages. They have been implemented in many Prolog systems. As such, they are deemed an worthy extension to the ISO/IEC 13211 Prolog standard.

This TR is an extension to the ISO/IEC 13211–1 Prolog standard, adopting a similar structure. Specifically, this TR either adds new sections and clauses to, or modifies the reading of existing clauses on ISO/IEC 13211–1.

This TR provides reference implementations for the specified built-in predicates and for a translator from grammar rules into Prolog clauses. In addition, it includes a comprehensive set of tests to help users and implementers check for compliance of Prolog systems. The source code of these reference implementations may be used without restrictions for any purpose.

This draft may contain in several places informative text, type-set in *italics*. Such informative text is used for editorial comments deemed useful during the development of this draft and may not be included in the final version.

Previous editors and draft documents

- Roger Scowen: *N171 — ISO/IEC DTR 13211–3:2004 Grammar rules in Prolog*, ISO, 2004-05

- Tony Dodd: *DCGs in ISO Prolog — A Proposal*, BSI, 1992

Contributors

This list needs to be completed; so far I've only included people present at the ISO meetings collocated with the ICLP (2005, 2006, and 2007) and the authors of the two drafts cited above, and Richard as I have included here some contributions from him that I found on the net.

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1 Scope

This TR is designed to promote the applicability and portability of Prolog grammar rules in data processing systems that support standard Prolog as defined in ISO/IEC 13211–1:1995. As such, this TR specifies:

a) The representation, syntax, and constraints of Prolog grammar rules

b) A logical expansion of grammar rules into Prolog clauses

    c) A set of built-in predicates for parsing with and expanding grammar rules

    d) Reference implementations and tests for the specified built-in predicates and for a grammar rule translator

NOTE — This part of ISO/IEC 13211 will supplement ISO/IEC 13211–1:1995.

2   Normative references

NOTE — No changes from the ISO/IEC 13211–1 Prolog standard.

3   Definitions

For the purposes of this TR, the following definitions are added to the ones specified in ISO/IEC 13211–1:

3.1   body (of a grammar-rule):   The second argument of a grammar-rule. A grammar-body-sequence, or a grammar-body-alternative, or a grammar-body-choice, or a grammar-body-element.

3.2   clause-term: A read-term `T.` in Prolog text where T does not have principal functor `(:-)/1` nor principal functor `(-->)/2`. (This definition replaces clause 3.33 of ISO/IEC 13211–1).

3.3   definite clause grammar: A sequence of grammar-rules.

3.4   expansion (of a grammar-rule):   The preparation for execution (cf. ISO/IEC 13211–1, section 7.5.1) of a grammar rule.

3.5   generating (wrt. a definite clause grammar):   Producing legal terminal-sequences of a grammar.

3.6   grammar-body-alternative: A compound term with principal functor `(;)/2` and each argument being a body (of a grammar-rule).

3.7   grammar-body-choice: A compound term with principal functor `(->)/2`. The first argument is a body (of a grammar-rule), and the second argument is a body.

3.8   grammar-body-element: A cut (the atom `!`), or a grammar-body-goal, or a non-terminal, or a terminal-sequence.

3.9   grammar-body-goal: A compound term with principal functor `({})/1` whose argument is a goal.

3.10   **grammar-body-sequence:**   A compound term with principal functor `(,)/2` and each argument being a body (of a grammar-rule).

3.11   **grammar-body-terminals:**   A terminal-sequence.

3.12   **grammar-rule:**   A compound term with principal functor `(-->)/2`.

3.13   **grammar-rule-term:**   A read-term `T.` where `T` is a grammar-rule.

3.14   **head (of a grammar-rule):**   The first argument of a grammar-rule. Either a non-terminal (of a grammar), or a compound term whose principal functor is `(,)/2`, the first argument is a non-terminal (of a grammar), and the second argument is a terminal-sequence.

3.15   **new variable with respect to a term T:**   A variable that is not an element of the variable set of `T`.

3.16   **non-terminal (of a grammar):**   An atom or compound term that denotes a non-terminal symbol of the grammar.

3.17   **non-terminal indicator:**   A compound term `A//N` where `A` is an atom and `N` is a non-negative integer, denoting one particular non-terminal.

3.18   **parsing (wrt. a definite clause grammar):**   Either rejecting illegal or successively accepting and consuming legal terminal-sequences, assigning them to corresponding non-terminals and obeying constraints by stake lists.

3.19   **terminal (of a grammar):**   Any Prolog term that denotes a terminal symbol of the grammar.

3.20   **terminal-sequence:**   A list (cf. ISO/IEC 13211–1, section 6.3.5) whose first argument, if any, is a terminal (of a grammar), and the second argument is a terminal-sequence.

3.21   **terminal-sequence, comprehensive:**   Terminal sequence containing as prefix a leading terminal-sequence which is entirely generated resp. parsed by a non-terminal.

3.22   **terminal-sequence, remaining:**   Rest of comprehensive terminal-sequence without the leading terminal-sequence corresponding to a non-terminal.

3.23   **variable, new with respect to a term T:**   See *new variable with respect to a term* `T`.

4 Symbols and abbreviations

NOTE — No changes from the ISO/IEC 13211–1 Prolog standard.

5 Compliance

5.1 Prolog processor

A conforming Prolog processor shall:

a) Correctly prepare for execution Prolog text which conforms to:

1. the requirements of this TR, and
2. the requirements of ISO/IEC 13211–1, and
3. the implementation defined and implementation specific features of the Prolog processor,

b) Correctly execute Prolog goals which have been prepared for execution and which conform to:

1. the requirements of this TR, and
2. the requirements of ISO/IEC 13211–1, and
3. the implementation defined and implementation specific features of the Prolog processor,

c) Reject any Prolog text or read-term whose syntax fails to conform to:

1. the requirements of this TR, and
2. the requirements of ISO/IEC 13211–1, and
3. the implementation defined and implementation specific features of the Prolog processor,

d) Specify all permitted variations from this TR in the manner prescribed by this TR and by the ISO/IEC 13211–1, and

e) Offer a strictly conforming mode which shall reject the use of an implementation specific feature in Prolog text or while executing a goal.

NOTE — This extends corresponding section of ISO/IEC 13211–1.

5.2 Prolog text

NOTE — No changes from the ISO/IEC 13211–1 Prolog standard.

5.3 Prolog goal

NOTE — No changes from the ISO/IEC 13211–1 Prolog standard.

5.4   Documentation

The corresponding section on the ISO/IEC 13211–1 Prolog standard is modified as follows:

A conforming Prolog processor shall be accompanied by documentation that completes the definition of every implementation defined and implementation specific feature specified in this TR and on the ISO/IEC 13211–1 Prolog standard.

5.5   Extensions

The corresponding section on the ISO/IEC 13211–1 Prolog standard is modified as follows:

A processor may support, as an implementation specific feature, any construct that is implicitly or explicitly undefined in this TR or on the ISO/IEC 13211–1 Prolog standard.

5.5.2   Predefined operators

Please see section 6.3 for the new predefined operators that this TR adds to the ISO/IEC 13211–1 Prolog standard.

6   Syntax

6.1   Notation

6.1.1   Backus Naur Form

No changes from the ISO/IEC 13211–1 Prolog standard.

6.1.2   Abstract term syntax

The text near the end of this section on the ISO/IEC 13211–1 Prolog standard is modified as follows:

Prolog text (6.2) is represented abstractly by an abstract list `x` where `x` is:

a) `d.t` where `d` is the abstract syntax for a directive, and `t` is Prolog text, or

b) `g.t` where `g` is the abstract syntax for a grammar rule, and `t` is Prolog text, or

c) `c.t` where `c` is the abstract syntax for a clause, and `t` is Prolog text, or

d) `nil`, the empty list.

The following section extends, with the specified number, the corresponding ISO/IEC 13211–1 section.

6.1.3 Variable names convention for terminal-sequences

This TR uses variables named `S0`, `S1`, ..., `S` to represent the terminal-sequences used as arguments when processing grammar rules or when expanding grammar rules into clauses. In this notation, the variables , `S1`, ..., `S` can be regarded as a sequence of states, with `S0` representing the initial state and the variable `S` representing the final state. Thus, if the variable S_i represents the initial terminal-sequence, the variable S_{i+1} will represent the remaining terminal-sequence after processing `Si` with a grammar rule.

6.2 Prolog text and data

The first paragraph of this section on ISO/IEC 13211–1 is modified as follows:

Prolog text is a sequence of read-terms which denote (1) directives, (2) grammar rules, and (3) clauses of user-defined procedures.

6.2.1 Prolog text

The corresponding section on the ISO/IEC 13211–1 is modified as follows:

Prolog text is a sequence of directive-terms, grammar-rule terms, and clause-terms.

```
          prolog text =   p text
```
Abstract: *pt*   *pt*
```
          p text =        directive term ,    p text
```
Abstract: *d.t*   *d*   *t*
```
          p text =        grammar rule term ,  p text
```
Abstract: *g.t*   *g*   *t*
```
          p text =        clause term ,        p text
```
Abstract: *c.t*   *c*   *t*
```
          p text =        ;
```
Abstract: *nil*

6.2.1.1 Directives

No changes from the ISO/IEC 13211–1 Prolog standard.

6.2.1.2 Clauses

The corresponding section on the ISO/IEC 13211–1 is modified as follows:

```
          clause term =                        term, end
```
Abstract: *c*   *c*
Priority: 1201
Condition: The principal functor of `c` is not `(:-)/1`
Condition: The principal functor of `c` is not `(-->)/2`

NOTE — Subclauses 7.5 and 7.6 defines how each clause becomes part of the database.

The following section extends, with the specified number, the corresponding ISO/IEC 13211–1 section:

6.2.1.3 Grammar rules

	grammar rule term =	term, end
Abstract:	*gt*	*gt*
Priority:	1201	
Condition:	The principal functor of `gt` is `(-->)/2`	
	grammar rule =	grammar rule term
Abstract:	*g*	*g*

NOTE — Section 10 of this TR defines how a grammar rule in Prolog text is expanded into an equivalent clause when Prolog text is prepared for execution.

6.3 Terms

NOTE — The operator `-->/2`, specified in section 6.3.4.4 of the ISO/IEC 13211–1 Prolog standard, is used as the principal functor of grammar rules.

7 Language concepts and semantics

The following section extends, with the specified number, the corresponding ISO/IEC 13211–1 section:

7.13 Predicate properties

The following implementation defined property is added to the list of predicate properties:

- `expanded_from(non_terminal, A//N)` — The predicate results from the expansion of a grammar rule for the non-terminal `A//N`

NOTE — the `expanded_from/2` property name was chosen in order to account for other possible, implementation-specific expansions.

7.14 Grammar rules

7.14.1 Terminals and non-terminals

Zero or more terminals are represented by terms contained in lists in order to distinguish them from non-terminals (string notation may be used as an alternative to lists when terminals are characters and the flag "double_quotes" has value "chars"; see sections 6.3.7 and 6.4.6 of ISO/IEC 13211–1). Non-terminals

are represented by callable terms.

NOTE — In the context of a grammar rule, *terminals* represent tokens of some language, and *non-terminals* represent sequences of tokens (see, respectively, sections 3.18 and 3.16).

7.14.2 Format of grammar rules

A grammar rule has the format:

```
GRHead --> GRBody.
```

A grammar rule is interpreted as stating that its head, `GRHead`, can be rewritten by its body, `GRBody`. The head and the body of grammar rules are constructed from *non-terminals* and *terminals*. The head of a grammar rule is a non-terminal or the conjunction of a non-terminal and, following, a terminal-sequence (a *stake list*, see 7.14.3):

```
NonTerminal --> GRBody.

NonTerminal, StakeList --> GRBody.
```

The control constructs that may be used on a grammar rule body are described in section 7.14.6. An empty grammar rule body is represented by an empty list:

```
GRHead --> [].
```

The empty list cannot be omitted, i.e. there is no `-->/1` form for grammar rules.

7.14.3 Stake lists

A *stake list* is a terminal-sequence, as an optional second argument of the head of a grammar rule (see 3.14). A stake list contains terminals that are prefixed to the remaining terminal-sequence after successful application of the grammar rule.

7.14.3.1 Examples

For example, assume that we need rules to *look-ahead* one or two tokens that would be consumed next. This could be easily accomplished by the following two grammar rules:

```
look_ahead(X),    [X]   --> [X].
look_ahead(X, Y), [X,Y] --> [X,Y].
```

When used for parsing, procedurally, these grammar rules can be interpreted as, respectively, consuming, and then restoring, one or two terminals.

7.14.4 Non-terminal indicator

A *non-terminal indicator* is a compound term with the format `//(A, N)` where `A` is an atom and `N` is a non-negative integer.

The non-terminal indicator `//(A, N)` indicates the grammar rule non-terminal whose functor is `A` and whose arity is `N`.

NOTES

1   In Prolog text, including ISO/IEC 13211–1 and this TR, a non-terminal indicator `//(A, N)` is normally written as `A//N`.

2   The concept of non-terminal indicator is similar to the concept of *predicate indicator* defined in sections 3.131 and 7.1.6.6 of the ISO/IEC 13211–1 Prolog. Non-terminal indicators may be used in exception terms thrown when processing or using grammar rules. In addition, non-terminal indicators may appear wherever a predicate indicator as defined in ISO/IEC 13211–1 can appear. Furthermore non-terminal indicators may be used as predicate property (cf. section 7.13). In particular, using non-terminal indicators in predicate directives allows the details of the expansion of grammar rules into Prolog clauses to be abstracted.

7.14.4.1   Examples

For example, given the following grammar rule:

```
sentence --> noun_phrase, verb_phrase.
```

The corresponding non-terminal indicator for the grammar rule left-hand side non-terminal is `sentence//0`. Assuming a `public/1` directive for declaring predicate scope, we could write:

```
:- public(sentence//0).
```

in order to be possible to use grammar rules for the non-terminal `sentence//0` outside its encapsulation unit.

7.14.5   Prolog goals in grammar rules

In the body of grammar rules, curly brackets enclose a sequence of Prolog goals that are executed when the grammar rule, prepared for execution, is processed.

NOTE — The ISO/IEC 13211–1 Prolog standard defines, in section 6.3.6, a *curly bracketed term* as a compound term with principal functor `'{}'/1`, whose argument may also be expressed by enclosing its argument in curly brackets.

7.14.5.1   Examples

Consider, for example, the following grammar rule:

```
digit(D) --> [C], {0'0 =< C, C =< 0'9, D is C - 0'0}.
```

This rule recognizes a single terminal as character code of a digit when the corresponding numeric value can be unified with the non-terminal argument.

7.14.6   Control constructs and built-in predicates supported by grammar rules

The following built-in predicates specified in the ISO/IEC 13211–1 Prolog standard may be used in the body of grammar rules: `\+/1`.

The following Prolog control constructs specified in the ISO/IEC 13211–1 Prolog standard may be used in the body of grammar rules, also outside of curly brackets (see 7.14.5), as control constructs: `(',')/2`, `(';')/2`, and `(!)/0`.

NOTE 1 — The effect of comma and semicolon, `(',')//2`, `(';')//2`, maybe understood best by application of `(write_canonical)/1` (see section 8.14.2.5 of ISO/IEC 13211–1) on a grammar rule, containing them:

```
?-write_canonical((sentence --> subject, verb, object;
                                 object, verb, subject)).

-->(sentence, ;(','(subject, ','(verb, object)),
               (','(object, ','(verb, subject)))))
yes
```

This leads to the following Prolog clause during preparation for execution :

```
sentence(CTS, RTS) :-
            subject(CTS, ITS1),
            verb(ITS1, ITS2),
            object(ITS2, RTS)
      ;
            object(CTS, ITS3),
            verb(ITS3, ITS4),
            subject(ITS4, RTS).
```

`ITS1 .. ITS4` are the respective intermediate terminal sequences, arising during continued parsing resp. generating the comprehensive terminal sequence `CTS` with two alternative forms.

NOTE 2 — A cut, `(!)//0`, placed as nonterminal at the end of the first alternative in this example, immediately before the semicolon, would commit the Prolog processor to the first alternative.

NOTE 3 — The behaviour of the control construct (`'->'`)`//2`, if any, and its preparation for execution shall be implementation specific.

The (`:`)`/2` control construct specified in the ISO/IEC 13211–2 Prolog standard may be used in the body of grammar rules (see 11.1.1).

The following Prolog control constructs and built-in predicates derived from control constructs specified in the ISO/IEC 13211–1 Prolog standard (sections 7.8 and 8.15) shall not be recognized as control constructs when used in a grammar rule body: `true/0`, `fail/0`, `repeat/0`, `call/1`, `once/1`, `catch/3`, and `throw/1`. When appearing in the place of a non-terminal, these Prolog control constructs and built-in predicates shall be interpreted as non-terminals respectively.:`true//0`, `fail//0`, `repeat//0`, `call//1`, `once//1`, `catch//3`, and `throw//1`. .

Expanding the non-terminal `call//1` shall lead to an expansion result `call/3` which is a legal goal for the control construct `call/3` which is required by this DTR and defined in 7.14.7.
A Prolog processor may support additional control constructs. Examples include *soft-cuts* and control constructs that enable the use of grammar rules stored on encapsulation units other than modules, such as objects. These additional control constructs must be treated as non-terminals by a Prolog processor working on a strictly conforming mode (see 5.1e).

NOTE — Consider the following example for the correlation of Grammar Rules, `call/1` and `call/3`:

```
atom_charsdiff(Atom, Xs0, Xs):-
    atom_chars(Atom, Chars),
    append(Chars, Xs, Xs0).

atomchars(Atom) --> call(atom_charsdiff(Atom)).

at_eos_pred([ ], [ ]).

at_eos --> call(at_eos_pred).
```

7.14.7   The non-terminal `call//1` and the control construct `call/3`

7.14.7.1   Description

The expansion of the non-terminal `call//1` leads to the control construct `call/3`. `call(G, A1, A2)` is true iff G is a goal which is true when activated using the

implementation defined arguments A1 and A2. For the definition of G, and Error cases restricted to G, see section 7.8.3 of ISO/IEC 13211-1.

For the definition of the arguments A1 and A2, examples and the error cases of `call/3` see the implementation specific documentation.

7.14.7.2 Description

```
call(+callable_term, ?argument1, ?argument2)
```

7.14.8 Executing procedures expanded from grammar rules

If a grammar rule to be prepared for execution has a non-terminal indicator N//A, and N is the name of the predicate indicator N/A' of a built-in predicate in the complete database, the result of expansion and the behaviour of the prepared grammar rule on execution is implementation dependent. This does not hold for the built-in predicates defined in 7.14.6.

When the database does not contain a grammar rule with non-terminal indicator N//A during execution of a non-terminal with non-terminal indicator N//A , the error term as specified in clause 7.7.7b of ISO/IEC 13211–1 when the flag `unknown` is set to `error` shall be:

```
existence_error(procedure, N//A)
```

NOTES

1   Prolog Processors shall report errors resulting from execution of grammar rules at the same abstraction level as grammar rules whenever possible.

2   Parsing resp. generating of texts with grammar rules is defined in sections 8.1.1 and 11.2. Grammar rules are expanded into Prolog clauses during preparation for execution, which maps the parsing or generating with a grammar rule body into executing a goal given a sequence of predicate clauses. See section 7.7 of ISO/IEC 13211–1 for details.

8   Built-in predicates

8.1   Grammar rule built-in predicates

8.1.1   phrase/3, phrase/2

8.1.1.1   Description

`phrase(GRBody, S0, S)` is true iff the grammar rule body `GRBody` successfully parses resp. generates, according to the currently defined grammar rules, the comprehensive terminal sequence `S0` unifying `S` with the remaining terminal sequence.

Procedurally, `phrase(GRBody, S0, S)` is executed by calling the Prolog goal corresponding to the expansion of the grammar rule body `GRBody`, given the terminal-sequences `S0` and `S`, according to the logical expansion of grammar rules described in section 10.

8.1.1.2   Template and modes

```
phrase(+callable_term, ?terminal-sequence, ?terminal-sequence)
```

8.1.1.3   Errors

  a) `GRBody` is a variable
     — `instantiation_error`

  b) `GRBody` is neither a variable nor a callable term
     — `type_error(callable, GRBody)`

  The following two errors are implementation defined, i.e. if a Prolog processor offers them, their form must be the following:

  c) `S0` is not a terminal-sequence
     — `type_error(terminal-sequence, S0)`

  d) `S` is not a terminal-sequence
     — `type_error(terminal-sequence, S)`

NOTE —   This relaxation is allowed because handling these errors could overburden a Prolog Processor.

8.1.1.4   Bootstrapped built-in predicates

The built-in predicate `phrase/2` provides similar functionality to `phrase/3`. The goal `phrase(GRBody, S0)` is true when all terminals in the terminal-sequence S0 are consumed and recognized resp. generated:

```
phrase(GRBody, S0) :-
    phrase(GRBody, S0, []).
```

8.1.1.5   Examples

These examples assume that the following grammar rules has been correctly prepared for execution and are part of the complete database:

```
determiner --> [the].
determiner --> [a].

noun --> [boy].
```

```
noun --> [girl].

verb --> [likes].
verb --> [scares].

sentence --> noun_phrase, verb_phrase.

noun_phrase --> determiner, noun.
noun_phrase --> noun.

verb_phrase --> verb.
verb_phrase --> verb, noun_phrase.
```

Some example calls of `phrase/2` and `phrase/3`:

```
| ?- phrase([the], [the]).

yes

| ?- phrase(sentence, [the, girl, likes, the, boy]).

yes

| ?- phrase(sentence, [the, girl, likes, the, boy, today]).

no

| ?- phrase(sentence, [the, girl, likes]).

no

| ?- phrase(sentence, Sentence).

Sentence = [the, girl, likes, the, boy]
yes

| ?- phrase(noun_phrase, [the, girl, scares, the, boy], Rest).

Rest = [scares, the, boy]
yes
```

9 Evaluable functors

NOTE — No changes from the ISO/IEC 13211–1 Prolog standard.

10   Logical expansion of grammar rules

This section extends, with the specified number, the ISO/IEC 13211–1 Prolog standard:

This section presents a logical view for the expansion of grammar rules into Prolog clauses, starting with a description of the used notation.

10.1   Notation

The terms `S0` and `S` represent, respectively, the comprehensive terminal-sequence and the remaining terminal-sequence after processing a grammar rule. Variables named S_i represent intermediate states, as explained in section 6.1.3.

The term $E_{Type}(T, S_i, S_{i+1})$ denotes an expansion of type *Type* of a term T, given, respectively, the comprehensive and remaining terminal-sequences S_i and S_{i+1}

Four types of expansion rules are used, denoted by the terms: E_{rule} (expansion of grammar rules), E_{body} (expansion of grammar rule bodies), $E_{terminals}$ (expansion of grammar rule terminals), and $E_{non\_terminal}$ (expansion of grammar rule non-terminals).

The symbol $\equiv$ is used to link a expansion rule with its resulting Prolog term or with another expansion rule.

10.2   Expanding a grammar rule

Grammar rules with a stake list:

E_{rule}((NonTerminal, Terminals --> GRBody), S0, S) $\equiv$ Head :- Body

where:

$E_{non\_terminal}$(NonTerminal, S0, S) $\equiv$ Head
E_{body}(GRBody, S0, S1), $E_{terminals}$(Terminals, S, S1) $\equiv$ Body

Grammar rule with no stake list:

E_{rule}((NonTerminal --> GRBody), S0, S) $\equiv$ Head :- Body

where:

$E_{non\_terminal}$(NonTerminal, S0, S) $\equiv$ Head
E_{body}(GRBody, S0, S) $\equiv$ Body

10.3   Expanding a non-terminal

$E_{non\_terminal}$(`NonTerminal, S0, S`) $\equiv$ `Head`

where:

```
NonTerminal =.. NonTerminalUniv,
append(NonTerminalUniv, [S0, S], HeadUniv),
Head =.. HeadUniv
```

(see section 11.3 for the definition of the auxiliary predicate `append/3`)

10.4   Expanding a terminal-sequence

Terminal-sequences, either a stake list or a grammar rule body goal:

$E_{terminals}$(`[], S0, S`) $\equiv$ `S0 = S`
$E_{terminals}$(`[T| Ts], S0, S`) $\equiv$ `S0 = [T| Tail]`

where:

$E_{terminals}$(`Ts, S1, S`) $\equiv$ `Tail`

where `S1` is a new variable with respect to the term `[T| Ts]`.

An alternative definition, given a terminal-sequence `Terminals` is:

$E_{terminals}$(`Terminals, S0, S`) $\equiv$ `S0 = List`

where:

```
append(Terminals, S, List)
```

(see section 11.3 for the definition of the auxiliary predicate `append/3`)

10.5   Expanding a grammar rule body

Non-instantiated variable on a grammar rule body:

E_{body}(`Var, S0, S`) $\equiv$ `phrase(Var, S0, S)`

If-then-else construct on the body of a grammar rule:

E_{body}(`(GRIf -> GRThen; GRElse), S0, S`) $\equiv$ `If -> Then; Else`

where:

E_{body}(`GRIf, S0, S1`) $\equiv$ `If`
E_{body}(`GRThen, S1, S`) $\equiv$ `Then`
E_{body}(`GRElse, S0, S`) $\equiv$ `Else`

If-then construct on the body of a grammar rule:

E_{body}(`(GRIf -> GRThen)`, `S0`, `S`) $\equiv$ `If -> Then`

where:

E_{body}(`GRIf, S0, S1`) $\equiv$ `If`
E_{body}(`GRThen, S1, S`) $\equiv$ `Then`

Disjunction on the body of a grammar rule:

E_{body}(`(GREither; GROr)`, `S0`, `S`) $\equiv$ `Either; Or`

where:

E_{body}(`GREither, S0, S`) $\equiv$ `Either`
E_{body}(`GROr, S0, S`) $\equiv$ `Or`

Conjunction on the body of a grammar rule:

E_{body}(`(GRFirst, GRSecond)`, `S0`, `S`) $\equiv$ `First, Second`

where:

E_{body}(`GRFirst, S0, S1`) $\equiv$ `First`
E_{body}(`GRSecond, S1, S`) $\equiv$ `Second`

Cut on the body of a grammar rule:

E_{body}(`!`, `S0`, `S`) $\equiv$ `!, S0 = S`

Curly-bracketed term on the body of a grammar rule:

E_{body}(`{}`, `S0`, `S`) $\equiv$ `S0 = S`
E_{body}(`{Goal}`, `S0`, `S`) $\equiv$ `Goal, S0 = S`

when `Goal` is a non-variable term and:

E_{body}(`{Goal}`, `S0`, `S`) $\equiv$ `call(Goal), S0 = S`

when `Goal` is a Prolog variable.

Negation on the body of a grammar rule:

E_{body}(`\+ Body`, `S0`, `S`) $\equiv$ `\+ Goal, S0 = S`

where:

E_{body}(Body, S0, S) $\equiv$ Goal

Terminal-sequence in the body of a grammar rule:

E_{body}(Terminals, S0, S) $\equiv E_{terminals}$(Terminals, S0, S)

Non-terminal on the body of a grammar rule:

E_{body}(NonTerminal, S0, S) $\equiv E_{non\_terminal}$(NonTerminal, S0, S)

11   Reference implementations

The reference implementations provided in this section do not preclude alternative or optimized implementations which express the syntax and semantics of this DTR. They serve for a better understanding of the DTR, but may also be used for free, to implement DCGs.

11.1   Grammar-rule translator

This section provides a reference implementation for a translator of grammar rules into Prolog clauses as specified in the ISO/IEC 13211–1 Prolog standard. The main idea is to translate grammar rules into clauses by adding two extra arguments to each grammar rule non-terminal, following the logical expansion of grammar rules, described in the previous section. The first extra argument is used for the comprehensive terminal-sequence. The second extra argument is used for the remaining terminal-sequence. This is a straight-forward solution. Nevertheless, compliance with this TR does not imply this specific translation solution, only compliance with the logical expansion, as specified in section 10.

This translator includes error-checking code that ensures that both the input grammar rule and the resulting clause are valid. In addition, this translator attempts to simplify the resulting clauses by removing redundant calls to `true/0` and by folding unifications. In some cases, the resulting clauses could be further optimized. Other optimizations can be easily plugged in, by modifying or extending the `dcg_simplify/4` predicate. However, implementers must be careful to delay output unifications in the presence of goals with side-effects such as cuts or input/output operations, ensuring the steadfastness of the generated clauses.

```
% converts a grammar rule into a normal clause:

dcg_rule(Rule, Clause) :-
    dcg_rule(Rule, S0, S, Expansion),
    dcg_simplify(Expansion, S0, S, Clause).
```

```prolog
dcg_rule((RHead --> _), _, _, _) :-
    var(RHead),
    throw(instantiation_error).

dcg_rule((RHead, _ --> _), _, _, _) :-
    var(RHead),
    throw(instantiation_error).

dcg_rule((_, Terminals --> _), _, _, _) :-
    var(Terminals),
    throw(instantiation_error).

dcg_rule((NonTerminal, Terminals --> GRBody), S0, S, (Head :- Body)) :-
    !,
    dcg_non_terminal(NonTerminal, S0, S, Head),
    dcg_body(GRBody, S0, S1, Goal1),
    dcg_terminals(Terminals, S, S1, Goal2),
    Body = (Goal1, Goal2).

dcg_rule((NonTerminal --> GRBody), S0, S, (Head :- Body)) :-
    !,
    dcg_non_terminal(NonTerminal, S0, S, Head),
    dcg_body(GRBody, S0, S, Body).

dcg_rule(Term, _, _, _) :-
    throw(type_error(grammar_rule, Term)).


% translates a grammar goal non-terminal:

dcg_non_terminal(NonTerminal, _, _, _) :-
    \+ callable(NonTerminal),
    throw(type_error(callable, NonTerminal)).

dcg_non_terminal(NonTerminal, S0, S, Goal) :-
    NonTerminal =.. NonTerminalUniv,
    append(NonTerminalUniv, [S0, S], GoalUniv),
    Goal =.. GoalUniv.


% translates a terminal-sequence:

dcg_terminals(Terminals, _, _, _) :-
    \+ is_proper_list(Terminals),
    throw(type_error(list, Terminals)).
```

```prolog
dcg_terminals(Terminals, S0, S, S0 = List) :-
    append(Terminals, S, List).


% translates a grammar rule body:

dcg_body(Var, S0, S, phrase(Var, S0, S)) :-
    var(Var),
    !.

dcg_body((GRIf -> GRThen), S0, S, (If -> Then)) :-
    !,
    dcg_body(GRIf, S0, S1, If),
    dcg_body(GRThen, S1, S, Then).

dcg_body((GREither; GROr), S0, S, (Either; Or)) :-
    !,
    dcg_body(GREither, S0, S, Either),
    dcg_body(GROr, S0, S, Or).

dcg_body((GRFirst, GRSecond), S0, S, (First, Second)) :-
    !,
    dcg_body(GRFirst, S0, S1, First),
    dcg_body(GRSecond, S1, S, Second).

dcg_body(!, S0, S, (!, S0 = S)) :-
    !.

dcg_body({}, S0, S, (S0 = S)) :-
    !.

dcg_body({Goal}, S0, S, (call(Goal), S0 = S)) :-
    var(Goal),
    !.

dcg_body({Goal}, _, _, _) :-
    \+ callable(Goal),
    throw(type_error(callable, Goal)).

dcg_body({Goal}, S0, S, (Goal, S0 = S)) :-
    !.

dcg_body(\+ GRBody, S0, S, (\+ Goal, S0 = S)) :-
    !,
    dcg_body(GRBody, S0, S, Goal).
```

```prolog
dcg_body([], S0, S, (S0=S)) :-
    !.

dcg_body([T| Ts], S0, S, Goal) :-
    !,
    dcg_terminals([T| Ts], S0, S, Goal).

dcg_body(NonTerminal, S0, S, Goal) :-
    dcg_non_terminal(NonTerminal, S0, S, Goal).


% simplifies the resulting clause:

dcg_simplify((Head :- Body), _, _, Clause) :-
    dcg_conjunctions(Body, Flatted),
    dcg_fold_left(Flatted, FoldedLeft),
    dcg_fold_pairs(FoldedLeft, FoldedPairs),
    (   FoldedPairs == true ->
        Clause = Head
    ;   Clause = (Head :- FoldedPairs)
    ).


% removes redundant calls to true/0 and flattens conjunction of goals:

dcg_conjunctions((Goal1 -> Goal2), (SGoal1 -> SGoal2)) :-
    !,
    dcg_conjunctions(Goal1, SGoal1),
    dcg_conjunctions(Goal2, SGoal2).

dcg_conjunctions((Goal1; Goal2), (SGoal1; SGoal2)) :-
    !,
    dcg_conjunctions(Goal1, SGoal1),
    dcg_conjunctions(Goal2, SGoal2).

dcg_conjunctions(((Goal1, Goal2), Goal3), Body) :-
    !,
    dcg_conjunctions((Goal1, (Goal2, Goal3)), Body).

dcg_conjunctions((true, Goal), Body) :-
    !,
    dcg_conjunctions(Goal, Body).

dcg_conjunctions((Goal, true), Body) :-
    !,
```

```
        dcg_conjunctions(Goal, Body).

    dcg_conjunctions((Goal1, Goal2), (Goal1, Goal3)) :-
        !,
        dcg_conjunctions(Goal2, Goal3).

    dcg_conjunctions(\+ Goal, \+ SGoal) :-
        !,
        dcg_conjunctions(Goal, SGoal).

    dcg_conjunctions(Goal, Goal).


    % folds left unifications:

    dcg_fold_left((Term1 = Term2), true) :-
        !,
        Term1 = Term2.

    dcg_fold_left(((Term1 = Term2), Goal), Folded) :-
        !,
        Term1 = Term2,
        dcg_fold_left(Goal, Folded).

    dcg_fold_left(Goal, Goal).


    % folds pairs of consecutive unifications (T1 = T2, T2 = T3):

    dcg_fold_pairs((Goal1 -> Goal2), (SGoal1 -> SGoal2)) :-
        !,
        dcg_fold_pairs(Goal1, SGoal1),
        dcg_fold_pairs(Goal2, SGoal2).

    dcg_fold_pairs((Goal1; Goal2), (SGoal1; SGoal2)) :-
        !,
        dcg_fold_pairs(Goal1, SGoal1),
        dcg_fold_pairs(Goal2, SGoal2).

    dcg_fold_pairs(((T1 = T2a), (T2b = T3)), (T1 = T3)) :-
        T2a == T2b,
        !.

    dcg_fold_pairs(((T1 = T2a), (T2b = T3), Goal), ((T1 = T3), Goal2)) :-
        T2a == T2b,
        !,
```

```
        dcg_fold_pairs(Goal, Goal2).

    dcg_fold_pairs((Goal1, Goal2), (Goal1, Goal3)) :-
        !,
        dcg_fold_pairs(Goal2, Goal3).

    dcg_fold_pairs(\+ Goal, \+ SGoal) :-
        !,
        dcg_fold_pairs(Goal, SGoal).

    dcg_fold_pairs(Goal, Goal).
```

11.1.1   Extended version for Prolog implementations with encapsulation mechanisms

Assuming that the infix operator `:/2` is used for calling predicates inside an encapsulation unit, the following clause would allow translation of grammar rule bodies that explicitly use non-terminals from another encapsulation unit:

```
    dcg_body(Unit:GRBody, S0, S, Unit:Goal) :-
        !,
        dcg_body(GRBody, S0, S, Goal).
```

One possible problem with this clause is that any existence errors when executing the goal `Unit:Goal` will most likely be expressed in terms of the expanded predicates and not in terms of the original grammar rule non-terminals. In order to more easily report errors at the same abstraction level as grammar rules, the following alternative clause may be used:

```
    dcg_body(Unit:GRBody, S0, S, Unit:phrase(GRBody, S0, S)) :-
        !,
        dcg_body(GRBody, S0, S, _).  % ensure that GRBody is valid
```

11.2   `phrase/3`

This section provides a reference implementation in Prolog of the built-in predicates `phrase/3`. It includes the necessary clauses for error handling, as specified in section 8.1.1.3. For the reference implementation of `phrase/2` see section 8.1.1.4.

```
    phrase(GRBody, S0, S) :-
        var(GRBody),
        throw(error(instantiation_error, phrase(GRBody, S0, S))).

    phrase(GRBody, S0, S) :-
        \+ callable(GRBody),
        throw(error(type_error(callable, GRBody), phrase(GRBody, S0, S))).
```

```
phrase(GRBody, S0, S) :-
    nonvar(S0),
    \+ is_list(S0),
    throw(error(type_error(list, S0), phrase(GRBody, S0, S))).

phrase(GRBody, S0, S) :-
    nonvar(S),
    \+ is_list(S),
    throw(error(type_error(list, S), phrase(GRBody, S0, S))).

phrase(GRBody, S0, S) :-
    dcg_body(GRBody, TS0, TS, Goal),
    TS0 = S0, TS = S,
    call(Goal).
```

The predicate `dcg_body/4` is part of the grammar rule translator reference implementation, defined in section 11.1. An alternative, informal implementation of `phrase/3` using a meta-interpreter is presented in the Annex A.

11.3   Auxiliary predicates used on the reference implementations

The following auxiliary predicates are used on the reference implementations:

```
append([], List, List).
append([Head| Tail], List, [Head| Tail2]) :-
    append(Tail, List, Tail2).

callable(Term) :-
    nonvar(Term),
    functor(Term, Functor, _),
    atom(Functor).

is_list([]) :-
    !.
is_list([_| Tail]) :-
    is_list(Tail).

is_proper_list(List) :-
    List == [], !.
is_proper_list([_| Tail]) :-
    nonvar(Tail),
    is_proper_list(Tail).
```

12 Test-cases for the reference implementations

12.1 Built-in predicates and user-defined hook predicates

```
% built-in predicates:
gr_pred_test(phrase(_, _,_), [built_in, static]).
gr_pred_test(phrase(_, _), [built_in, static]).

% simple test predicate:
test_gr_preds :-
    write('Testing existence of built-in predicates'), nl,
    write('and user-defined hook predicates...'), nl, nl,
    gr_pred_test(Pred, ExpectedProps),
    functor(Pred, Functor, Arity),
    write('Testing predicate '), write(Functor/Arity), nl,
    write('  Expected properties: '), write(ExpectedProps), nl,
    findall(Prop, predicate_property(Pred, Prop), ActualProps),
    write('  Actual properties: '), write(ActualProps), nl,
    fail.
test_gr_preds.
```

12.2 `phrase/2-3` built-in predicate tests

Tests needed!

12.3 Grammar-rule translator tests

Know any hard to translate grammar rules? Contribute them!

When checking compliance of a particular grammar rule translator, results of the tests in this section must be compliant with the logical expansion of grammar rules, as specified in section 10.

```
% terminal tests with list notation:
gr_tr_test(101, (p --> []), success).
gr_tr_test(102, (p --> [b]), success).
gr_tr_test(103, (p --> [abc, xyz]), success).
gr_tr_test(104, (p --> [abc | xyz]), error).
gr_tr_test(105, (p --> [[], {}, 3, 3.2, a(b)]), success).
gr_tr_test(106, (p --> [_]), success).

% terminal tests with string notation:
gr_tr_test(151, (p --> "b"), success).
gr_tr_test(152, (p --> "abc", "q"), success).
gr_tr_test(153, (p --> "abc" ; "q"), success).
```

```
% simple non-terminal tests:
gr_tr_test(201, (p --> b), success).
gr_tr_test(202, (p --> 3), error).
gr_tr_test(203, (p(X) --> b(X)), success).

% conjunction tests:
gr_tr_test(301, (p --> b, c), success).
gr_tr_test(311, (p --> true, c), success).
gr_tr_test(312, (p --> fail, c), success).
gr_tr_test(313, (p(X) --> call(X), c), success).

% disjunction tests:
gr_tr_test(351, (p --> b ; c), success).
gr_tr_test(352, (p --> q ; []), success).
gr_tr_test(353, (p --> [a] ; [b]), success).

% if-then-else tests:
gr_tr_test(401, (p --> b -> c), success).
gr_tr_test(411, (p --> b -> c; d), success).
gr_tr_test(421, (p --> b -> c1, c2 ; d), success).
gr_tr_test(422, (p --> b -> c ; d1, d2), success).
gr_tr_test(431, (p --> b1, b2 -> c ; d), success).
gr_tr_test(441, (p --> [x] -> [] ; q), success).

% negation tests:
gr_tr_test(451, (p --> \+ b, c), success).
gr_tr_test(452, (p --> b, \+ c, d), success).

% cut tests:
gr_tr_test(501, (p --> !, [a]), success).
gr_tr_test(502, (p --> b, !, c, d), success).
gr_tr_test(503, (p --> b, !, c ; d), success).
gr_tr_test(504, (p --> [a], !, {fail}), success).
gr_tr_test(505, (p(a), [X] --> !, [X, a], q), success).
gr_tr_test(506, (p --> a, ! ; b), success).

% {}/1 tests:
gr_tr_test(601, (p --> {b}), success).
gr_tr_test(602, (p --> {3}), error).
gr_tr_test(603, (p --> {c,d}), success).
gr_tr_test(604, (p --> '{}'((c,d))), success).
gr_tr_test(605, (p --> {a}, {b}, {c}), success).
gr_tr_test(606, (p --> {q} -> [a] ; [b]), success).
gr_tr_test(607, (p --> {q} -> [] ; b), success).
gr_tr_test(608, (p --> [foo], {write(x)}, [bar]), success).
gr_tr_test(609, (p --> [foo], {write(hello)},{nl}), success).
```

```
gr_tr_test(610, (p --> [foo], {write(hello), nl}), success).

% "metacall" tests:
gr_tr_test(701, (p --> X), success).
gr_tr_test(702, (p --> _), success).

% non-terminals corresponding to "graphic" characters
% or built-in operators/predicates:
gr_tr_test(801, ('[' --> b, c), success).
gr_tr_test(802, ('=' --> b, c), success).

% stakelist tests:
gr_tr_test(901, (p, [t] --> b, c), success).
gr_tr_test(902, (p, [t] --> b, [t]), success).
gr_tr_test(903, (p, [t] --> b, [s, t]), success).
gr_tr_test(904, (p, [t] --> b, [s], [t]), success).
gr_tr_test(905, (p(X), [X] --> [X]), success).
gr_tr_test(906, (p(X, Y), [X, Y] --> [X, Y]), success).
gr_tr_test(907, (p(a), [X] --> !, [X, a], q), success).
gr_tr_test(908, (p, [a,b] --> [foo], {write(hello), nl}), success).
gr_tr_test(909, (p, [t1], [t2] --> b, c), error).
gr_tr_test(910, (p, b --> b), error).
gr_tr_test(911, ([t], p --> b), error).
gr_tr_test(911, ([t1], p, [t2] --> b), error).


% simple expand_term/2 test predicate:

test_gr_tr :-
    write('Testing expand_term/2 predicate...'), nl, nl,
    gr_tr_test(N, GR, Result),
    write(N), write(':  '), writeq(GR), write('  ---  '),
    write(Result), write(' expected'), nl,
    (   catch(
            expand_term(GR, Clause),
            Error,
            (write('  error: '), write(Error), nl, fail)) ->
        write('  '), writeq(Clause)
    ;   write('  expansion failed!')
    ),
    nl, nl,
    fail.

test_gr_tr.
```

```
% simple predicate for dumping test grammar rules into a file:
% (restricted to rules whose expansion is expected to succeed)

create_gr_file :-
    write('Creating grammar rules file "gr.pl" ...'),
    open('gr.pl', write, Stream),
    (   gr_tr_test(N, GR, success),
        write(Stream, '% '), write(Stream, N),
        write(Stream, ':'), nl(Stream),
        write_canonical(Stream, GR), write(Stream, '.'),
        nl(Stream), fail
    ;   close(Stream)
    ),
    write(' created.'), nl.
```

A   phrase/3 meta-interpreter

Note that this alternative reference implementation makes it simple to report existence errors at the same abstraction level as grammar rules.

```
phrase(GRBody, S0, S) :-
    phrase(GRBody, Cont, S0, S1),
    (   Cont == {} ->
        S = S1
    ;   Cont = !(SBody),
        !,
        phrase(SBody, S1, S)
    ).

phrase(GRBody, _, S0, S) :-
    var(GRBody),
    throw(error(instantiation_error, phrase(GRBody, S0, S))).

phrase(GRBody, _, S0, S) :-
    \+ callable(GRBody),
    throw(error(type_error(callable, GRBody), phrase(GRBody, S0, S))).

phrase(GRBody, _, S0, S) :-
    nonvar(S0),
    \+ is_list(S0),
    throw(error(type_error(list, S0), phrase(GRBody, S0, S))).

phrase(GRBody, _, S0, S) :-
    nonvar(S),
    \+ is_list(S),
```

```
    throw(error(type_error(list, S), phrase(GRBody, S0, S))).

phrase(!, Cont, S0, S) :-
    !,
    Cont = !({}),
    S = S0.

phrase((GRBody1, GRBody2), Cont, S0, S) :-
    !,
    phrase(GRBody1, ContGRBody1, S0, S1),
    (   ContGRBody1 == {} ->
        phrase(GRBody2, Cont, S1, S)
    ;   ContGRBody1 = !(SGRBody1),
        Cont = !((SGRBody1, GRBody2)),
        S = S1
    ).

phrase(\+ GRBody, Cont, S0, S) :-
    !,
    \+ phrase(GRBody, S0, S),
    Cont = {},
    S0 = S.

phrase((GRBody1; GRBody2), Cont, S0, S) :-
    !,
    (    phrase(GRBody1, Cont, S0, S)
    ;    phrase(GRBody2, Cont, S0, S)
    ).

phrase((GRBody1 -> GRBody2), Cont, S0, S) :-
    !,
    phrase(GRBody1, S0, S1),
    phrase(GRBody2, Cont, S1, S).


phrase({}, Cont, S0, S) :-
    !,
    Cont = {},
    S = S0.

phrase({Goal}, Cont, S0, S) :-
    !,
    call(Goal),
    Cont = {},
    S = S0.
```

```
phrase([], Cont, S0, S) :-
    !,
    Cont = {},
    S = S0.

phrase([Head| Tail], Cont, S0, S) :-
    !,
    append([Head| Tail], S, S0),
    Cont = {}.

phrase(GRHead, _, S0, S) :-
    \+ dcg_clause(GRHead --> _),
    current_prolog_flag(unknown, Value),
    (    Value == fail ->
         fail
    ;    Value == warning ->
         % implementation-defined warning
    ;    functor(GRHead, NonTerminal, Arity),
         throw(error(
             existence_error(procedure, NonTerminal//Arity),
             phrase(GRHead, S0, S)))
    ).

phrase(GRHead, {}, S0, S) :-
    dcg_clause(GRHead, GRBody),
    phrase(GRBody, ContY, S0, S1),
    (    ContY == {} ->
         S = S1
    ;    ContY = !(SBody),
         !,
         phrase(SBody, S1, S)
    ).
```