Optimizing Compilers

Inter-Procedural Dataflow Analysis

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Svntax

 P_{\star} ::= begin $D_{\star} S_{\star}$ end $D \quad ::= \quad D; D \mid \operatorname{proc} p(\operatorname{val} x; \operatorname{res} y) \operatorname{is}^{\ell_n} S \operatorname{end}^{\ell_x}$ S ::= ... | [call p(a,z)] $_{\ell}^{\ell_c}$

Labeling scheme

• procedure declarations

 ℓ_n : for entering the body

 ℓ_x : for exiting the body

• procedure calls

 ℓ_c : for the call

 ℓ_r : for the return

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Analysing Procedures

We consider procedures with call-by-value and call-by-result parameters.

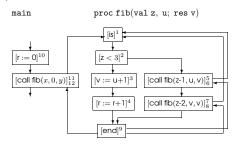
Example:

```
proc fib(val z,u; res v) is
     if z<3 then
       (v:=u+1; r:=r+1)
       call fib (z-1,u,v);
       call fib (z-2,v,v)
  end.
r:=0;
call fib(x,0,y)
```

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Example Flow Graph

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Flow Graph for Procedures

	$[\operatorname{call} p(a,z)]_{\ell_r}^{\ell_c}$	$\operatorname{proc} p(\operatorname{val} x; \operatorname{res} y) \operatorname{is}^{\ell_n} S \operatorname{end}^{\ell_x}$
init	ℓ_c	ℓ_n
final	$\{\ell_r\}$	$\{\ell_x\}$
blocks	$\{[\operatorname{call} p(a,z)]_{\ell_r}^{\ell_c}\}$	$\{is^{\ell_n}\} \cup blocks(S) \cup \{end^{\ell_x}\}$
labels	$\{\ell_c,\ell_r\}$	$\{\ell_c,\ell_r\} \cup labels(S)$
flow	$\{(\ell_c; \ell_n), (\ell_x; \ell_r)\}$	$\{(\ell_n,init(S))\} \cup flow(S) \cup \{\ell,\ell_x) \mid \ell \in final(S))\}$

- $(\ell_c; \ell_n)$ is the flow corresponding to calling a procedure at ℓ_c and entering the procedure body at ℓ_n and
- $(\ell_x; \ell_r)$ is the flow corresponding to exiting a procedure body at ℓ_x and returning to the call at ℓ_r .

Naive Formulation

Treat the three kinds of flow, (ℓ_1, ℓ_2) , $(\ell_c; \ell_n)$, $(\ell_x; \ell_r)$ in the same v

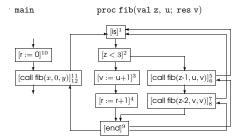
Equation system:

$$\begin{array}{rcl} A_{\circ}(\ell) & = & \bigsqcup\{A_{\bullet}(\ell') \mid (\ell',\ell) \in F \lor (\ell';\ell) \in F\} \sqcup \iota_E^{\ell} \\ A_{\bullet}(\ell) & = & f_{\ell}^{A}(A_{\circ}(\ell)) \end{array}$$

- both procedure calls $(\ell_c; \ell_n)$ and procedure returns $(\ell_x; \ell_r)$ of treated like "goto's".
- there is no mechanism for ensuring that information flowing $(\ell_c; \ell_n)$ flows back along $(\ell_x; \ell_r)$ to the same call
- intuitively, the equation system considers a much too large "paths" through the program and hence will be grossly imp (although formally on the safe side)

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Matching Procedure Entries and Exits



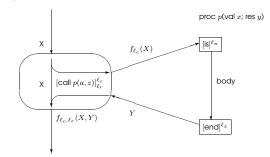
We want to overcome the shortcoming of the naive formulation by restricting attention to paths that have the proper nesting of procedure calls and exits.

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General Formulation: Calls and Returns



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"Meet" over Valid Paths (MVP)

· A complete path from ℓ_1 to ℓ_2 in P_\star has proper nesting of proceentries and exits; and a procedure returns to the point where it called:

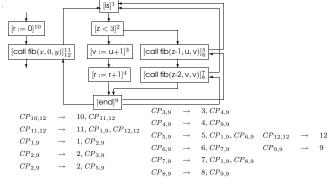
$$\begin{array}{ll} CP_{\ell_1,\ell_2} \longrightarrow \ell_1 & \text{whenever } \ell_1 = \ell_2 \\ \\ CP_{\ell_1,\ell_3} \longrightarrow \ell_1, CP_{\ell_2,\ell_3} & \text{whenever } (\ell_1,\ell_2) \in \mathsf{flow}_\star \\ \\ CP_{\ell_c,\ell} \longrightarrow \ell_c, CP_{\ell_n,\ell_x}, CP_{\ell_r,\ell} & \text{whenever} P_\star \text{ contains } [\mathsf{call} \; p(a,z)] \end{array}$$

Definition: $(\ell_c, \ell_n, \ell_r, \ell_x) \in \text{interflow}_\star \text{ if } P_\star \text{ contains } [\text{call } p(a, z)]_{\ell_r}^{\ell_c} \text{ cas proc } p(\text{val } x : \text{ res } v) \text{ is}^{\ell_n} S \text{ end}^{\ell_x}$

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and proc $p(\text{val }x; \text{ res }y) \text{ is }^{\ell_n} S \text{ end}$

Example



Some valid paths: (10,11,1,2,3,4,9,12) and (10,11,1,2,5,1,2,3,4,9,6,7,1,2,3,4,9,8,9,12)

A non-valid path: (10,11,1,2,5,1,2,3,4,9,12)

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Valid Paths

A valid path starts at the entry node init, of P_{\star} , all the procedure exits match the procedure entries but some procedures might be entered but not yet exited:

$VP_{\star} \longrightarrow VP_{init_{\star},\ell}$	whenever $\ell \in Lab_\star$
$VP_{\ell_1,\ell_2} \longrightarrow \ell_1$	whenever $\ell_1=\ell_2$
$VP_{\ell_1,\ell_3} \longrightarrow \ell_1, VP_{\ell_2,\ell_3}$	whenever $(\ell_1,\ell_2)\in \text{flow}_\star$
$VP_{\ell_c,\ell} \longrightarrow \ell_c, CP_{\ell_n,\ell_x}, VP_{\ell_r,\ell}$	whenever P_{\star} contains $[\operatorname{call}p(a,z)]_{\ell_r}^{\ell_c}$
	and proc $p(\operatorname{val} x; \operatorname{res} y) \operatorname{is}^{\ell_n} S \operatorname{end}^{\ell_x}$
$VP_{\ell_c,\ell} \longrightarrow \ell_c, VP_{\ell_n,\ell}$	whenever P_{\star} contains $[\operatorname{call}p(a,z)]_{\ell_r}^{\ell_c}$
	and proc $p(\operatorname{val} x; \operatorname{res} y) \operatorname{is}^{\ell_n} S \operatorname{end}^{\ell_x}$

MVP Solution

$$\mathit{MVP}_{\circ}(\ell) = \bigsqcup \{ f_{\vec{\ell}}(\iota) | \vec{\ell} \in \mathit{vpath}_{\circ}(\ell) \}$$

$$MVP_{\bullet}(\ell) = |\{f_{\vec{\ell}}(\iota)|\vec{\ell} \in vpath_{\bullet}(\ell)\}$$

where

$$vpath_{\circ}(\ell)=\{[\ell_1,\ldots,\ell_{n-1}]\mid n\geq 1\wedge \ell_n=\ell\wedge [\ell_1,\ldots,\ell_n] \text{ is valid path }$$

$$\mathit{vpath}_{\bullet}(\ell) = \{[\ell_1, \dots, \ell_n] \mid n \geq 1 \land \ell_n = \ell \land [\ell_1, \dots, \ell_n] \text{ is valid path} \}$$

The MVP solution may be undecidable for lattices satisfying the Aing Chain Condition, just as was the case for the MOP solution.

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Making Context Explicit

- The MVP solution may be undecidable for lattices of finite height (as was the case for the MOP solution)
- We have to reconsider the MFP solution and avoid taking too many invalid paths into account
- Encode information about the paths taken into data flow properties themselves
- Introduce context information

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MFP Counterpart

Context sensitive analysis: add context information

- call strings:
 - an abstraction of the sequences of procedure calls that have been performed so far
 - example: the program point where the call was initiated
- assumption sets:

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- an abstraction of the states in which previous calls have been performed
- example: an abstraction of the actual parameters of the call

Context insensitive analysis: take no context information into account.

Abstracting Call Strings

Problem: call strings can be arbitrarily long (recursive calls)

Solution: truncate the call strings to have length of at most k for some fixed number k

- $\Delta = \mathsf{Lab}^{\leq k}$
- k=0: context insensitive analysis
 - Λ (the call string is the empty string)
- ullet k=1: remember the last procedure call
 - $-\Lambda$, [11], [5], [7]
- k=2: remember the last two procedure calls
 - $-\Lambda$, [11], [11, 5], [11, 7], [5, 5], [5, 7], [7, 5], [7, 7]

References

- Material for this 5th lecture www.complang.tuwien.ac.at/knoop/oue185187_ws0910.html
- Book

Flemming Nielson, Hanne Riis Nielson, Chris Hankin:

Principles of Program Analysis.

Springer, (450 pages, ISBN 3-540-65410-0), 1999.

- Chapter 2 (Data Flow Analysis)

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Call Strings as Context

- Encode the path taken
- Only record flows of the form (ℓ_c, ℓ_n) corresponding to a pro-
- we take as context $\Lambda = Lab^*$ where the most recent label ℓ procedure call is at the right end
- Elements of ∧ are called call strings
- The sequence of labels $\ell_c^1, \ell_c^2, \dots, \ell_c^n$ is the call string leading current call which happened at ℓ_c^1 ; the previous calls where $\ell_c^2 \dots \ell_c^n$. If n=0 then no calls have been performed so far.

For the example program the following call strings are of interes Λ , [11], [11, 5], [11, 7], [11, 5, 5], [11, 5, 7], [11, 7, 5], [11, 7, 7], ...

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