Motivation: Von Verifikation über Analyse zur Transformation – Optimierung am Beispiel "code motion"-basierter Transformationen (Teil 1)

Analyse und Verifikation (WS 2006/2007) / 7. Teil (05.12.2006)

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Why Considering Code Motion (CM)? (1)

...because it is

- Relevant ...widely used in practice
- General ...a family of optimizations rather than a single one
- Well-understood ...manually proven correct and optimal
- Challenging ...conceptually simple, but exhibits lots of thought-provoking phenomena

Why Considering Code Motion (CM)? (2)

Last but not least, it is...

- Truly classical ... has a long history
 - Morel, E. and Renvoise, C. Global Optimization by Suppression of Partial Redundancies. CACM 22 (2), 96 - 103, 1979.
 - Ershov, A. P. On Programming of Arithmetic Operations. CACM 1 (8), 3 6, 1958.

Conceptually

...code motion can be considered a two-stage process

1. Expression hoisting

...hoisting expressions to "earlier" safe computation points

2. Total redundancy elimination

...eliminating computations which became totally redundant



Correctness, Optimality

We can prove...

• Correctness

Theorem ["Essence"]

...at every use site of a temporary, recomputing the expression yields the same value which is stored in the temporary

• Optimality

Theorem [Earliestness principle]

...hoisting expressions to their earliest safe computation points leads to computationally optimal programs → ...known as Busy Code Motion (PLDI'92, Knoop et al.)

Note

Traditionally,

- Code (C) means expressions
- Motion (M) means hoisting

But...

• CM is more than hoisting of expressions and PR(E)E!





Towards the Design Space of CM-Algorithms...

More generally...

- Code means expressions/assignments
- Motion means hoisting/sinking

Code / Motion	Hoisting	Sinking	
Expressions	EH	•/•	
Assignments	AH	AS	







...while taking New Challenges of Program Optimization into Account

...there is more than speed!

1999 World Market for Microprocessors

Chip Category	Number Sold		
Embedded 4-bit	2000 million		
Embedded 8-bit	4700 million		
Embedded 16-bit	700 million		
Embedded 32-bit	400 million		
DSP	600 million		
Desktop 32/64-bit	150 million		

... David Tennenhouse (Intel Director of Research). Keynote Speech at the 20th IEEE Real-Time Systems Symposium (RTSS'99), Phoenix, Arizona, December 1999.

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Think of...

... domain-specific processors as used in embedded systems

• Telecom

- Cell phones, pagers, ...
- Consumer Electronics
 - MP3 player, cameras, pocket games, ...

• Automative

- GPS navigation, airbags, ...
- ...

Code for Embedded Systems

Requirements...

- Performance (often real-time constraints)
- Code size (system-on-chip, on-chip RAM/ROM)

• ...

For embedded systems...

...code size is often more critical than speed!

Code for Embedded Systems (Cont'd)

Requirements ...and how they are commonly addressed:

- Assembly programming
- Manual postpass optimizations

Shortcomings...

- Error-prone
- Extended time-to-market

... problems getting even worse with increasing complexity.

Hence, we observe...

...a trend towards HLL programming (C/C++)

Given this trend...

...how does traditional compiler and optimizer technology support the specific requirement profile of code for embedded systems?

Code Size

Run-Time Performance

Unfortunately, little.

As a Matter of Fact...

Traditional optimizations...

- ...are strongly biased towards performance optimization
- ...are not code-size sensitive and usually don't offer any control about their impact on code size

In the following, we demonstrate this considering

• Partial Redundancy (Expression) Elimination (PR(E)E)

as example.









As we have observed already: Conceptually...

PRE can be considered a two-stage process...

1. Expression hoisting

...hoisting expressions to "earlier" safe computation points

2. Total redundancy elimination

...eliminating computations becoming totally redundant

Extreme Strategy – Earliestness Principle

Placing computations as early as possible...

• Theorem [Computational Optimality]

...hoisting expressions to their earliest safe computation points yields computationally optimal programs

 \sim ...known as Busy Code Motion (PLDI'92, Knoop et al.)

...already known to Morel and Renvoise (though no theorem or proof).

Earliestness Principle

Placing computations as early as possible...

... yields computationally optimal programs.







For comparison, the previous program

...computationally optimal, too, but mininum register pressure!



Dual Extreme Strategy – Latestness Principle

Placing computations as late as possible...

• Theorem [Optimality]

...hoisting expressions to their latest safe computation points yields computationally optimal programs with minimum register pressure

 \sim ...known as Lazy Code Motion (PLDI'92, Knoop et al.)



These days...

Lazy Code Motion is...

. . .

- ...the de-facto standard algorithm for PRE used in contemporary state-of-the-art compilers
 - Gnu compiler family
 - Sun Sparc compiler family





Towards Code-Size Sensitive PRE...

• Background: Classical PRE

- → Busy CM (BCM) / Lazy CM (LCM) (Knoop et al., PLDI'92)
 - Received the ACM SIGPLAN Most Influential PLDI Paper Award 2002 (for 1992)
 - Selected for "20 Years of the ACM SIGPLAN PLDI: A Selection" (60 papers out of ca. 600 papers)
- Code-Size Sensitive PRE (Knoop et al., POPL'00)
 - \rightsquigarrow ...modular extension of BCM/LCM
 - * Modelling and Solving the Problem

...based on graph-theoretical means

* Main Results

...correctness, optimality







The Running Example (Cont'd)

Note, we do not want the following transformation: It's no option!



Code-Size Sensitive PRE

\rightsquigarrow The Problem

...how to get a code-size minimal placement of computations, i.e., a placement which is

- admissible (semantics & performance preserving)
- code-size minimal

\rightsquigarrow Solution: A Fresh Look at PRE

...considering PRE a trade-off problem: trading the original computations against newly inserted ones!

\rightsquigarrow The Clou: Use Graph Theory!

...reducing the trade-off problem to the computation of tight sets in bipartite graphs based on maximum matchings!





Apparently

Off-the-shelf algorithms of graph theory can be used to compute...

- Maximum matchings and
- Tight sets

Hence, our **PRE** problem boils down to...

...constructing the bipartite graph modelling the problem!







DownSafety Closures

DownSafety Closure

For $n \in DownSafe/Upsafe$ the DownSafety Closure Closure(n) is the smallest set of nodes satisfying

- 1. $n \in Closure(n)$
- 2. $\forall m \in \underline{Closure}(n) \setminus Comp. \ succ(m) \subseteq \underline{Closure}(n)$
- 3. $\forall m \in Closure(n)$. $pred(m) \cap Closure(n) \neq \emptyset \Rightarrow$ $pred(m) \setminus UpSafe \subseteq Closure(n)$



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DownSafety Regions

Some subsets of nodes are distinguished. We call each of these sets a DownSafety Region...

- A set $\mathcal{R} \subseteq N$ of nodes is a DownSafety Region if and only if
 - 1. $Comp \setminus UpSafe \subseteq \mathcal{R} \subseteq DownSafe \setminus UpSafe$
 - 2. $Closure(\mathcal{R}) = \mathcal{R}$

The Key Questions

...concerning correctness and optimality:

1. Where to insert computations, why is it correct?

2. What is the impact on the code size?

3. Why is it optimal, i.e., code-size minimal?

...three theorems answering one of these questions each.

Main Results / First Question

1. Where to insert computations, why is it correct?

Intuitively, at the earliestness frontier of the DS-region induced by the tight set...

Theorem 1 [Tight Sets: Insertion Points]

Let $TS \subseteq S_{DS}$ be a tight set. Then $\mathcal{R}_{TS} =_{df} \Gamma(TS) \cup (Comp \setminus UpSafe)$ is a DownSafety Region with $Body_{\mathcal{R}_{TS}} = TS$

Correctness

...immediate corollary of Theorem 1 and Insertion Theorem

Main Results / Second Question

2. What is the impact on the code size?

Intuitively, the difference between computations inserted and replaced...

Theorem 2 [DownSafety Regions: Space Gain]

Let \mathcal{R} be a DownSafety Region

with $Body_{\mathcal{R}} =_{df} \mathcal{R} \setminus EarliestFrontier_{\mathcal{R}}$

Then

• Space Gain of Inserting at EarliestFrontier $_{\mathcal{R}}$:

 $\begin{aligned} |\textit{Comp} \setminus \textit{UpSafe}| &- |\textit{EarliestFrontier}_{\mathcal{R}}| = \\ |\textit{Body}_{\mathcal{R}}| &- |\Gamma(\textit{Body}_{\mathcal{R}})| \quad _{df} = \textit{defic}(\textit{Body}_{\mathcal{R}}) \end{aligned}$

Main Results / Third Question

3. Why is it optimal, i.e., code-size minimal?

Due to an inherent property of tight sets (non-negative deficiency!)...

Optimality Theorem [The Transformation]

Let $TS \subseteq S_{DS}$ be a tight set.

• Insertion Points:

Insert_{SpCM} = $_{df}$ EarliestFrontier_{R_{TS}} = $\mathcal{R}_{TS} \setminus TS$

• Space Gain:

 $\operatorname{defic}(TS) =_{df} |TS| - |\Gamma(TS)| \ge 0$ max.

Largest vs. Smallest Tight Sets: The Impact

Code-Size Sensitive PRE at a Glance

Choice of Priority	Apply	То	Using	Yields	Auxiliary Information Required		
LQ		Not meaningful: The identity, i.e., G itself is optimal!					
SQ	Subsumed by $\mathcal{SQ} > \mathcal{CQ}$ and $\mathcal{SQ} > \mathcal{LQ}!$						
CQ	BCM	G			$\tt UpSafe(G), DownSafe(G)$		
$\mathcal{CQ} > \mathcal{LQ}$	LCM	G		$\mathbf{LCM}(G)$	$\mathtt{UpSafe}(G),\mathtt{DownSafe}(G),\mathtt{Delay}(G)$		
$\mathcal{SQ} > \mathcal{CQ}$	SpCM	G	Largest tight set	$\mathbf{SpCM}_{LTS}(\mathbf{G})$	$\tt UpSafe(G), \tt DownSafe(G)$		
$\mathcal{SQ} > \mathcal{LQ}$	SpCM	G	Smallest tight set		UpSafe(G), DownSafe(G)		
CQ > SQ	SpCM	LCM(G)	Largest tight set		$\label{eq:upSafe} \begin{array}{c} \texttt{UpSafe}(G), \texttt{DownSafe}(G), \texttt{Delay}(G) \\ \texttt{UpSafe}(\mathbf{LCM}(G)), \texttt{DownSafe}(\mathbf{LCM}(G)) \end{array}$		
$\mathcal{CQ} > \mathcal{SQ} > \mathcal{LQ}$	SpCM	$\mathbf{LCM}(G)$	Smallest tight set		$\label{eq:upSafe} \begin{array}{c} \texttt{UpSafe}(G), \texttt{DownSafe}(G), \texttt{Delay}(G) \\ \texttt{UpSafe}(\mathbf{LCM}(G)), \texttt{DownSafe}(\mathbf{LCM}(G)) \end{array}$		
SQ > CQ > LQ	\mathbf{SpCM}	$\mathbf{DL}(\mathbf{SpCM}_{LTS}(\mathbf{G}))$	Smallest tight set		$\begin{array}{c} \texttt{UpSafe}(G), \texttt{DownSafe}(G), \\ \texttt{Delay}(\mathbf{SpCM}_{LTS}(G)), \\ \texttt{UpSafe}(\mathbf{DL}(\mathbf{SpCM}_{LTS}(G))), \end{array}$		

Conclusions, Perspectives

A brief survey of PRE...

- 1958: ...first glimpse of PRE
 - → Ershov's work on On Programming of Arithmetic Operations.
- 1979: ...origin of contemporary PRE
 - $\rightsquigarrow\,$ Morel/Renvoise's seminal work on PRE
- 1992: ...LCM [Knoop et al., PLDI'92]
 - \rightsquigarrow ...first to achieve comp. optimality with minimum register pressure
 - \rightsquigarrow ...first to rigorously be proven correct and optimal
- 2000: ...origin of code-size sensitive PRE [Knoop et al., POPL 2000]
 - \rightsquigarrow ...first to allow prioritization of goals
 - \rightsquigarrow ...rigorously be proven correct and optimal
 - \rightsquigarrow ...first to bridge the gap between traditional compilation and compilation for embedded systems

Conclusions, Perspectives (Cont'd)

• ca. since 1997: ...a new strand of research on PRE

→ Speculative PRE: Gupta, Horspool, Soffa, Xue, Scholz, Knoop,...

- **2005**: ...another fresh look at PRE (as maximum flow problem)
 - → Unifying PRE and Speculative PRE [Jingling Xue and J. Knoop]

Another Look at the History of PRE

- < 1979 ... Special Techniques
 - \rightsquigarrow Total Redundancy Elimination, Loop Invariant Code Motion
- **1979** ... Partial Redundancy Elimination
 - → **Pioneering** ... Morel/Renvoise's bidirectional algorithm [1979]
 - → Heuristic improvements … Dhamdhere [1988, 1991], Drechsler/Stadel [1988], Sorkin [1989], Dhamdhere/Rosen/Zadeck [1992], …
- 1992 ... BCM & LCM [Knoop et al., PLDI'92]
 - → BCM ... first to achieve Computational Optimality: Earliestness Principle
 - → LCM ... first to achieve Comp. & Lifetime Optimality: Latestness Principle
 - ... first to be purely unidirectional, however, not yet code-size sensitive.
- 2000/2004: Code-Size Sensitive PRE [Knoop et al., POPL 2000, LCTES 2004]
- 2005: Unifying PRE and Speculative PRE [Jingling Xue and Knoop]