Today's Topic

Parsing: Lexical and syntactical analysis

- Combinator parsing
- Monadic parsing

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Lexical and Syntactical Analysis

• ...in the following summarized as parsing

...an application of functional programming typically used to demonstrate its power and elegance.

Enjoys a long history. As an example of early work see e.g...

• W. Burge. *Recursive Programming Techniques*, Addison-Wesley, 1975.

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Parsing – Implementation Variants

Two variants...

- Combinator parsing
 - → recursive descent parsing
 - Graham Hutton. Higher-Order Functions for Parsing. Journal of Functional Programming 2(3):323-343, 1992.
- Monadic parsing
 - Graham Hutton, Erik Meijer. Monadic Parser Combinators. Technical Report NOTTCS-TR-96-4, Dept. of Computer Science, University of Nottingham, 1996.

Reference

The following presentation is based on...

- Chapter 17
 Simon Thompson. Haskell The Craft of Functional Programming, Addison-Wesley, 2nd edition, 1999.
- Graham Hutton, Erik Meijer. *Monadic Parsing in Haskell*. Journal of Functional Programming 1(1), 1993.

Parsing informally

The basic problem...

- Read a sequence of objects of type a and
- extract from this sequence an object or a list of objects of type b.

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Initial Considerations 1(2)

What should be the type of a parsing function?

We have to answer...

How shall the parser behave if there ...

- ...are multiple results?
- ...is a failure?

Example: Parsing of Expressions

Consider...

Expressions

The parsing task to be solved...

• Read an expression of the form ((2+3)*5) and yield the corresponding expression of type expr.

(Note: This can be considered the reverse of the show function. It is similar to the derived read function, but differs in the arguments it takes (expressions of the form ((2+3)*5) vs. expressions of the form Op Mul (Add (Lit 2) (Lit 3)) (Lit 5)).

Initial Considerations 2(2)

Now we have to answer...

What shall be done with the remaining input?

Type of the Parser 1(2)

The conclusion of our initial considerations...

Remark:

- The capability of delivering multiple results enables the analysis of ambiguous grammars
 - → list of successes technique
- Each element in the output list represents a successful parse.

Basic Parsers 1(3)

Primitive, input-independent parsing functions

• The always failing parsing function

```
none :: Parse a b
none inp = []
```

• The always successful parsing function

```
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Remark:

- The none parser always fails. It does not accept anything.
- \bullet The succeed parser does not consume its input. In BNF-notation this corresponds to the symbol ε representing the empty word.

Type of the Parser 2(2)

Convention:

- Delivery of the empty list ...signals failure of the analysis.
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component is the input not yet considered.

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Basic Parsers 2(3)

Primitive, input-dependent parsing functions

• Recognizing single objects (token)...

• Recognizing single objects satisfying a particular property...

Basic Parsers 3(3)

Application:

```
bracket = token '('
dig = spot isDigit

isDigit :: Char -> Bool
  isDigit ch = ('0' <= ch) && (ch <= '9')

Note: ...token can be defined by means of spot
  token t = spot (== t)</pre>
```

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Combining Parsers 2(4)

• Sequential composition of parsers

Underlying intuition:

...an operator expression starts with a bracket *followed by* a number

Combining Parsers 1(4)

...to obtain (more) complex parsing functions

→ Combinator Parsing

...building a library of higher-order polymorphic functions, which are then used to construct parsers

Alternatives

```
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp
```

Underlying intuition:

 \ldots an expression is *either* a literal, *or* a variable *or* an operator expression

Example:

```
(bracket 'alt' dig) "234" --> [] ++ [(2,"34")]
```

 \sim ...the alt parser combines the results of the parses given by parsers p1 and p2

Combining Parsers 3(4)

Example:

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Combining Parsers 4(4)

• Transformation/Modification

 \sim change the item returned by the parser, or build something from it...

```
build :: Parse a b \rightarrow (b \rightarrow c) \rightarrow Parse a c build p f inp = [ (f x, rem) | (x,rem) \leftarrow p inp ]
```

Example: (digList returns a list of numbers and shall be embedded such that the number represented by it is returned.)

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Example: A Parser for a List of Objects

We suppose to be given a parser recognizing single objects:

Intuition:

- A list can be empty.
 - \rightarrow this is recognized by the parser succeed []
- A list can be non-empty, i.e., it consists of an object followed by a list of objects.
- \rightarrow this is recognized by the combined parser p >*> list p, where we use build to turn a pair (x,xs) into the list (x:xs).

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The combinators

- alt
- >*>
- build

together with the basic parsers constitute a universal "parser basis," i.e., allow to build any parser which might be desired.

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Summary and Conclusion

...about combining parsers (parser combinators)

- Parsing functions in the above fashion are structurally similar to grammars in BNF-form. For each operator of the BNF-grammar there is a corresponding (higher-order) parsing function.
- These higher-order functions *combine* simple(r) parsing functions to (more) complex parsing functions.
- They are thus also called *combining forms*, or, as a short hand, *combinators* (cf. Graham Hutton. *Higher-Order Functions for Parsing*).

Overview of the Parsing Functions 1(4)

```
-- Sequence operator
infixr 5 >*>
-- Parser type
type Parse a b = [a] -> [(b,[a])]
-- Input-independent parsing functions
none :: Parse a b
none inp = []
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

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Overview of the Parsing Functions 2(4)

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Overview of the Parsing Functions 3(4)

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```
-- Alternatives
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp

-- Sequences
(>*>) :: Parse a b -> Parse a c -> Parse a (b,c)
(>*>) p1 p2 inp
= [((y,z),rem2) | (y,rem1) <- p1 inp, (z,rem2) <- p2 rem1]

-- Transformation/Modification
build :: Parse a b -> (b -> c) -> Parse a c
build p f inp = [ (f x, rem) | (x,rem) <- p inp]
```

Overview of the Parsing Functions 4(4)

Application: Back to the Initial Example

We consider expressions of the form...

```
data Expr = Lit Int | Var Name | Op Ops Expr Expr
data Ops = Add | Sub | Mul | Div | Mod

Op Add (Lit 2) (Lit 3) corresponds to 2+3
```

...where the following convention shall hold:

- \bullet *Literals* ...67, \sim 89, etc., where \sim is used for unary minus
- Names ...the lower case characters from 'a' to 'z'
- Applications of the binary operations ...+, *, -, /, %, where % is used for mod and / for integer division.
- Expressions are fully bracketed, and white space is not permitted.

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A Parser for Expressions 2(3)

Part II: Parsing (fully bracketed binary) operator expressions

```
opExpParse
= (token '(' >*>
    parser >*>
    spot isOp >*>
    parser >*>
    token ')')
    'build' makeExpr
```

Part III: Parsing literals (numerals)

A Parser for Expressions 1(3)

The parser consists...

```
parser :: Parse Char Expr
parser = litParse 'alt' nameParse 'alt' opExpParse
```

... of three parts corresponding to the three sorts of expressions.

Part I: Parsing names of variables

```
nameParse :: Parse Char Expr
nameParse = spot isName 'build' Name
isName :: Char -> Bool
isName x = ('a' <= x && x <= 'z')</pre>
```

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A Parser for Expressions 3(3)

```
neList :: Parse a b -> Parse a [b] optional :: Parse a b -> Parse a [b]
```

such that:

- neList p recognizes a non-empty list of the objects which are recognized by p
- optional p recognizes an object recognized by p or succeeds immediately.

Note that neList and optional as well as a number of other supporting functions used such as...

- isOp
- charlistToExpr
- .

are yet to be defined (\rightarrow exercise).

The Top-level Parser / Putting it all together

Converting a string to the expression it represents...

Note:

- The input string is provided by the value of inp.
- The parse is successful, if the result contains at least one parse, in which all the input has been read.

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Summary and Conclusions 2(2)

The following language features proved invaluable...

- Higher-order functions ...Parse a b is of a functional type; all parser combinators are thus higher-order functions, too.
- Polymorphism ...consider again the type of Parse a b: We do need to be specific about either the input or the output type of the parsers we build. Hence, the above parser combinator can immediately be reused for other (token-) and data types.
- Lazy evaluation ... "on demand" generation of the possible parses, automatical backtracking (the parsers will backtrack through the different options until a successful one is found).

Summary and Conclusions 1(2)

Parsers of the form...

```
type Parse a b = [a] -> [(b,[a])]

none :: Parse a b
succeed :: b -> Parse a b
spot :: (a -> Bool) -> Parse a a
alt :: Parse a b -> Parse a b
>*> :: Parse a b -> Parse a c -> Parse a (b,c)
build :: Parse a b -> (b -> c) -> Parse a c
topLevel :: Parse a b -> [a] -> b
```

...support particularly well the construction of so-called *recursive descent* parsers.

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Monadic Parsing

```
newtype Parser a = Parser (String -> [(a,String)])
```

We use again the convention:

- Delivery of the empty list ...signals failure of the analysis
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component the input still to be examined

A Monad of Parsers

Basic Parsers...

• Recognizing single characters...

Compare: item VS. token

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Properties of return and (>>=)

As required for instances of class Monad, we can show...

```
return a >>= f = f a

p >>= return = p

p >>= (\a -> (f a >>= g)) = (p >>= (\a -> f a)) >>= g
```

Reminder:

- The above properties are required for each instance of class Monad, not just for the specific instance of the parser monad
 - ...return is left-unit and right-unit for (>>=)
 → ...allows a simpler and more concise definition of some parsers
 - ...(>>=) is associative
 - \sim ...allows suppression of parentheses when parsers are applied sequentially

The Parser Monad

```
Reminder: The class monad...
```

Compare: return vs. succeed and (>>=) vs. infixr

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Typical Structure of a Parser 1(2)

...using the operator (>>=)

```
p1 >>= \a1 ->
p2 >>= \a2 ->
...
pn >>= \an ->
f a1 a2 ... an
```

Intuition

There is a natural operational reading of such a parser...

- Apply parser p1 and denote its result value a1
- Apply subsequently parser p2 and denote its result value a2
- .
- Apply concludingly parser pn and denote its result value an
- Combine finally the intermediate result values by applying some suitable function f

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Typical Structure of a Parser 2(2)

The do-notation allows a more elegant and appealing notation...

```
do a1 <- p1
   a2 <- p2
   ...
   an <- pn
   f a1 a2 ... an</pre>
```

Alternatively, in just one line...

```
do {a1 <- p1; a2 <- p2; ...; an <- pn; f a1 a2 ... an}
```

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Remark:

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A generator of the form ai <- pi can be

Notational Conventions

• ai <- pi are called *generators*

Expressions of the form

• replaced by pi, if the generated value will not be used afterwards

(since they generate values for the variables ai)

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Example

A Parser p, which...

- reads three characters
- drops the second character of these and
- \bullet returns the first and the third character as a pair

Implementation:

```
p :: Parser (Char, Char)
p = do {c <- item; item; d <- item; return (c,d)}</pre>
```

Parser Extensions 1(2)

Monads with a *zero* and a plus are captured by two built-in class definitions in Haskell...

```
class Monad m => MonadZero m where
   zero :: m a

class MonadZero m => MonadPlus m where
   (++) :: m a -> m a -> m a
```

Parser Extensions 2(2)

The type constructor Parser can be made instances of these two classes as follows:

• The parser which always fails...

```
instance MonadZero Parser where
zero = Parser (\cs -> [])
```

• The parser which non-deterministically selects...

```
instance MonadPlus Parser where p ++ q = (\cs -> parse p cs ++ parse q cs)
```

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Simple Properties 2(2)

Specifically for the parser monad we can additionally show...

```
zero >>= f = zero
p >>= const zero = zero
    (p ++ q) >>= f = (p >>= f) ++ (q >>= f)
p >>= (\a -> f a ++ g a) = (p >>= f) ++ (p >>= g)
```

Informally:

- ...zero is left-zero and right-zero element for (>>=)
- ...(>>=) distributes through (++)

Simple Properties 1(2)

We can show...

```
zero ++ p = p
p ++ zero = p
p ++ (q ++ r) = (p ++ q) ++ r
```

Remark: The above properties are required to hold for each monad with zero and plus

Informally:

- ...zero is left-unit and right-unit for (++)
- ...(++) is associative

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Deterministic Selection

The parser which deterministically selects...

Note:

- (+++) shows the same behavior as (++), but yields at most one result
- (+++) satisfies all of the previously mentioned properties of (++)

Further Parsers

Recognizing...

• single objects satisfying a particular property

```
sat :: (Char -> Bool) -> Parser Char
sat p = do {c <- item; if p c then return c else zero}</pre>
```

• single objects

```
char :: Char -> Parser Char
char c = sat (c ==)
```

• sequences of numbers, lower case and upper case characters, etc.

...analogously to char

Compare: sat and char VS. spot and token

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Recursion Combinators 2(3)

• Similar to the parser many but with interspersed applications of the parser sep, whose result values are thrown away

Recursion Combinators 1(3)

Useful parsers can often recursively be defined...

Parse a specific string

```
string :: String -> Parser String
string "" = return ""
string (c:cs) = do {char c; string cs; return (c:cs)}
```

• Parse repeated applications of a parser p

```
(Zero or more applications of p)
many :: Parser a -> Parser [a]
many p = many1 p +++ return []

(One or more applications of p)
many1 :: Parser a -> Parser [a]
many1 p = do {a <- p; as <- many p; return (a:as)}</pre>
```

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Recursion Combinators 3(3)

 Parse repeated applications of a parser p, separated by applications of a parser op, whose result value is an operator that is assumed to associate to the left, and which is used to combine the results from the p parsers

Lexical Combinators

Suitable combinators allow suppression of a lexical analysis (token recognition), which traditionally precedes parsing...

• Parsing of a string with blanks and line breaks

```
space :: Parser String
space = many (sat isSpace)
```

• Parsing of a token by means of parsers p

```
token :: Parser a -> Parser a
token p = do {a <- p; space; return a}</pre>
```

• Parsing of a symbol token

```
symb :: String -> Parser String
symb cs = token (string cs)
```

• Application of parser p, removal of initial blanks

```
apply :: Parser a -> String -> [(a,String)]
apply p = parse (do {space; p}]
```

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Example: Parsing of Expressions 2(3)

Parsing and evaluating expressions (yielding integer values) using the chainl1 combinator to implement the left-recursive production rules for expr and term...

```
expr :: Parser Int
addop :: Parser (Int -> Int -> Int)
mulop :: Parser (Int -> Int -> Int)

expr = term 'chainl1' addop
term = factor 'chainl1' mulop
factor = digit +++ do {symb "("; n <- expr; symb ")"; return n}
digit = do {x <- token (sat isDIgit); return (ord x - ord '0')}

addop = do {symb "+"; return (+)} +++ do {symb "-"; return (-)}
mulop = do {symb "*"; return (*)} +++ do {symb "/"; return (div)}</pre>
```

Example: Parsing of Expressions 1(3)

Grammar:

...for arithmetic expressions built up from single digits using the operators +, -, *, /, and parentheses:

```
expr ::= expr addop term | term
term ::= term mulop factor | factor
factor ::= digit | (expr)
digit ::= 0 | 1 | ... | 9

addop ::= + | -
mulop ::= * | /
```

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Example: Parsing of Expressions 3(3)

Example:

Evaluating

```
apply expr " 1 - 2 * 3 + 4 " gives the singleton list [(-1,"")] as desired
```

as desired.

Further Readings 1(3)

On combinator parsing...

- J. Fokker, Functional Parsers, In: Advanced Functional Programming, First International Summer School, Springer. LNCS 925 (1995), 1-23.
- S. Hill. Combinators for Parsing Expressions. Journal of Functional Programming 6:445-463, 1996.
- P. Koopman, R. Plasmeijer, Efficient Combinator Parsers. In Proceedings of Implementation of Functional Languages, Springer, LNCS 1595 (1999), 122-138.

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Further Readings 3(3)

On parser libraries...

- Daan Leijen, Erik Meijer. Parsec: A Practical Parser Library. Electronic Notes in Theoretical Computer Science 41(1), 2001.
- A. Gill, S. Marlow. Happy The Parser Generator for Haskell. University of Glasgow, 1995.

http://www.haskell.org/happy

Further Readings 2(3)

On error-correcting parsing...

- P. Wadler. How to Replace Failure with a List of Successes, in: Functional Programming Languages and Computer Architectures, Springer, LNCS 201 (1985), 113 - 128.
- D. Swierstra, P. Azero Alcocer, Fast, Error Correcting Parser Combinators: A Short Tutorial. In Proceedings SOF-SEM'99. Theory and Practice of Informatics, 26th Seminar on Current Trends in Theory and Practice of Informatics, Springer, LNCS 1725 (1999), 111-129.
- D. Swierstra, L. Duponcheel. Deterministic, Error Correcting Combinator Parsers. In: Advanced Functional Programming, Second International Spring School, Springer. LNCS 1129 (1996), 184-207.

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Next Course Meeting...

• Thu, May 26, 2011, lecture time: 4.15 p.m. to 5.45 p.m., lecture room on the ground floor of the building Argentinierstr. 8