#### Today's Topic

Parsing: Lexical and syntactical analysis

- Combinator parsing
- Monadic parsing

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

-1

#### 1

#### Lexical and Syntactical Analysis

• ...in the following summarized as parsing

...an application of functional programming typically used to demonstrate its power and elegance.

Enjoys a long history. As an example of early work see e.g...

• W. Burge. *Recursive Programming Techniques*, Addison-Wesley, 1975.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

2

#### Parsing – Implementation Variants

Two variants...

- Combinator parsing
  - → recursive descent parsing
  - Graham Hutton. Higher-Order Functions for Parsing. Journal of Functional Programming 2(3):323-343, 1992.
- Monadic parsing
  - Graham Hutton, Erik Meijer. Monadic Parser Combinators. Technical Report NOTTCS-TR-96-4, Dept. of Computer Science, University of Nottingham, 1996.

#### Reference

The following presentation is based on...

- Chapter 17
   Simon Thompson. Haskell The Craft of Functional Programming, Addison-Wesley, 2nd edition, 1999.
- Graham Hutton, Erik Meijer. *Monadic Parsing in Haskell*. Journal of Functional Programming 1(1), 1993.

#### Parsing informally

The basic problem...

- Read a sequence of objects of type a and
- extract from this sequence an object or a list of objects of type b.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

\_\_

# **Initial Considerations 1(2)**

What should be the type of a parsing function?

We have to answer...

How shall the parser behave if there ...

- ...are multiple results?
- ...is a failure?

#### **Example: Parsing of Expressions**

Consider...

Expressions

The parsing task to be solved...

• Read an expression of the form ((2+3)\*5) and yield the corresponding expression of type expr.

(Note: This can be considered the reverse of the show function. It is similar to the derived read function, but differs in the arguments it takes (expressions of the form ((2+3)\*5) vs. expressions of the form Op Mul (Add (Lit 2) (Lit 3)) (Lit 5)).

# **Initial Considerations 2(2)**

Now we have to answer...

• What shall be done with the remaining input?

#### Type of the Parser 1(2)

The conclusion of our initial considerations...

#### Remark:

- The capability of delivering multiple results enables the analysis of ambiguous grammars
  - → list of successes technique
- Each element in the output list represents a successful parse.

#### Basic Parsers 1(3)

Primitive, input-independent parsing functions

• The always failing parsing function

```
none :: Parse a b
none inp = []
```

• The always successful parsing function

```
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

#### Remark:

- The none parser always fails. It does not accept anything.
- $\bullet$  The succeed parser does not consume its input. In BNF-notation this corresponds to the symbol  $\varepsilon$  representing the empty word.

# Type of the Parser 2(2)

Convention:

- Delivery of the empty list ...signals failure of the analysis.
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component is the input not yet considered.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

10

#### Basic Parsers 2(3)

Primitive, input-dependent parsing functions

• Recognizing single objects (token)...

• Recognizing single objects satisfying a particular property...

# Basic Parsers 3(3)

Application:

```
bracket = token '('
dig = spot isDigit

isDigit :: Char -> Bool
  isDigit ch = ('0' <= ch) && (ch <= '9')

Note: ...token can be defined by means of spot
  token t = spot (== t)</pre>
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

# Combining Parsers 2(4)

• Sequential composition of parsers

Underlying intuition:

...an operator expression starts with a bracket *followed by* a number

#### Combining Parsers 1(4)

...to obtain (more) complex parsing functions

→ Combinator Parsing

...building a library of higher-order polymorphic functions, which are then used to construct parsers

Alternatives

```
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp
```

Underlying intuition:

...an expression is either a literal, or a variable or an operator expression

Example:

```
(bracket 'alt' dig) "234" --> [] ++ [(2,"34")]
```

 $\sim$  ...the alt parser combines the results of the parses given by parsers p1 and p2

# Combining Parsers 3(4)

Example:

13

15

#### Combining Parsers 4(4)

• Transformation/Modification

 $\sim$  change the item returned by the parser, or build something from it...

```
build :: Parse a b \rightarrow (b \rightarrow c) \rightarrow Parse a c build p f inp = [ (f x, rem) | (x,rem) \leftarrow p inp ]
```

Example: (digList returns a list of numbers and shall be embedded such that the number represented by it is returned.)

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

17

#### **Example: A Parser for a List of Objects**

We suppose to be given a parser recognizing single objects:

#### Intuition:

- A list can be empty.
  - $\rightarrow$  this is recognized by the parser succeed []
- A list can be non-empty, i.e., it consists of an object followed by a list of objects.
  - $\rightarrow$  this is recognized by the combined parser p >\*> list p, where we use build to turn a pair (x,xs) into the list (x:xs).

#### The Clou

The combinators

- alt
- >\*>
- build

together with the basic parsers constitute a universal "parser basis," i.e., allow to build any parser which might be desired.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

18

#### **Summary and Conclusion**

...about combining parsers (parser combinators)

- Parsing functions in the above fashion are structurally similar to grammars in BNF-form. For each operator of the BNF-grammar there is a corresponding (higher-order) parsing function.
- These higher-order functions *combine* simple(r) parsing functions to (more) complex parsing functions.
- They are thus also called *combining forms*, or, as a short hand, *combinators* (cf. Graham Hutton. *Higher-Order Functions for Parsing*).

# Overview of the Parsing Functions 1(4)

```
-- Sequence operator
infixr 5 >*>
-- Parser type
type Parse a b = [a] -> [(b,[a])]
-- Input-independent parsing functions
none :: Parse a b
none inp = []
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

# Overview of the Parsing Functions 2(4)

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

22

# Overview of the Parsing Functions 3(4)

21

23

```
-- Alternatives
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp

-- Sequences
(>*>) :: Parse a b -> Parse a c -> Parse a (b,c)
(>*>) p1 p2 inp
= [((y,z),rem2) | (y,rem1) <- p1 inp, (z,rem2) <- p2 rem1]

-- Transformation/Modification
build :: Parse a b -> (b -> c) -> Parse a c
build pf inp = [ (f x, rem) | (x,rem) <- p inp]
```

# Overview of the Parsing Functions 4(4)

#### **Application: Back to the Initial Example**

We consider expressions of the form...

```
data Expr = Lit Int | Var Name | Op Ops Expr Expr
data Ops = Add | Sub | Mul | Div | Mod

Op Add (Lit 2) (Lit 3) corresponds to 2+3
```

...where the following convention shall hold:

- $\bullet$  *Literals* ...67,  $\sim$ 89, etc., where  $\sim$  is used for unary minus
- Names ...the lower case characters from 'a' to 'z'
- Applications of the binary operations ...+, \*, -, /, %, where % is used for mod and / for integer division.
- Expressions are fully bracketed, and white space is not permitted.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

25

#### A Parser for Expressions 2(3)

Part II: Parsing (fully bracketed binary) operator expressions

```
opExpParse
= (token '(' >*>
    parser >*>
    spot isOp >*>
    parser >*>
    token ')')
    'build' makeExpr
```

Part III: Parsing literals (numerals)

#### A Parser for Expressions 1(3)

The parser consists...

```
parser :: Parse Char Expr
parser = litParse 'alt' nameParse 'alt' opExpParse
```

... of three parts corresponding to the three sorts of expressions.

#### Part I: Parsing names of variables

```
nameParse :: Parse Char Expr
nameParse = spot isName 'build' Name
isName :: Char -> Bool
isName x = ('a' <= x && x <= 'z')</pre>
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

26

# A Parser for Expressions 3(3)

```
neList :: Parse a b -> Parse a [b] optional :: Parse a b -> Parse a [b]
```

such that:

- neList p recognizes a non-empty list of the objects which are recognized by p
- optional p recognizes an object recognized by p or succeeds immediately.

Note that neList and optional as well as a number of other supporting functions used such as...

- isOp
- charlistToExpr
- ..

are yet to be defined ( $\rightarrow$  exercise).

# The Top-level Parser / Putting it all together

Converting a string to the expression it represents...

#### Note:

- The input string is provided by the value of inp.
- The parse is successful, if the result contains at least one parse, in which all the input has been read.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

20

#### **Summary and Conclusions 2(2)**

The following language features proved invaluable...

- Higher-order functions ...Parse a b is of a functional type; all parser combinators are thus higher-order functions, too.
- Polymorphism ...consider again the type of Parse a b: We do need to be specific about either the input or the output type of the parsers we build. Hence, the above parser combinator can immediately be reused for other (token-) and data types.
- Lazy evaluation ... "on demand" generation of the possible parses, automatical backtracking (the parsers will backtrack through the different options until a successful one is found).

#### **Summary and Conclusions 1(2)**

Parsers of the form...

```
type Parse a b = [a] -> [(b,[a])]

none :: Parse a b
succeed :: b -> Parse a b
spot :: (a -> Bool) -> Parse a a
alt :: Parse a b -> Parse a b
>*> :: Parse a b -> Parse a c -> Parse a (b,c)
build :: Parse a b -> (b -> c) -> Parse a c
topLevel :: Parse a b -> [a] -> b
```

...support particularly well the construction of so-called *recursive descent* parsers.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

30

#### **Monadic Parsing**

```
newtype Parser a = Parser (String -> [(a,String)])
```

We use again the convention:

- Delivery of the empty list ...signals failure of the analysis
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component the input still to be examined

#### A Monad of Parsers

Basic Parsers...

• Recognizing single characters...

Compare: item VS. token

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

33

#### Properties of return and (>>=)

As required for instances of class Monad, we can show...

```
return a >>= f = f a

p >>= return = p

p >>= (\a -> (f a >>= g)) = (p >>= (\a -> f a)) >>= g
```

#### Reminder:

- The above properties are required for each instance of class Monad, not just for the specific instance of the parser monad
  - ...return is left-unit and right-unit for (>>=)
     → ...allows a simpler and more concise definition of some parsers
  - ...(>>=) is associative
    - $\sim$  ...allows suppression of parentheses when parsers are applied sequentially

#### The Parser Monad

```
Reminder: The class monad...
```

Compare: return vs. succeed and (>>=) vs. infixr

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

24

# Typical Structure of a Parser 1(2)

...using the operator (>>=)

```
p1 >>= \a1 ->
p2 >>= \a2 ->
...
pn >>= \an ->
f a1 a2 ... an
```

#### Intuition

There is a natural operational reading of such a parser...

- Apply parser p1 and denote its result value a1
- Apply subsequently parser p2 and denote its result value a2
- .
- Apply concludingly parser pn and denote its result value an
- Combine finally the intermediate result values by applying some suitable function f

#### Typical Structure of a Parser 2(2)

The do-notation allows a more elegant and appealing notation...

```
do a1 <- p1
   a2 <- p2
   ...
   an <- pn
   f a1 a2 ... an</pre>
```

Alternatively, in just one line...

```
do {a1 <- p1; a2 <- p2; ...; an <- pn; f a1 a2 ... an}
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

37

39

#### **Notational Conventions**

Expressions of the form

• ai <- pi are called *generators* (since they generate values for the variables ai)

#### Remark:

A generator of the form ai <- pi can be

• replaced by pi, if the generated value will not be used afterwards

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

38

#### Example

A Parser p, which...

- reads three characters
- drops the second character of these and
- returns the first and the third character as a pair

Implementation:

```
p :: Parser (Char, Char)
p = do {c <- item; item; d <- item; return (c,d)}</pre>
```

# Parser Extensions 1(2)

Monads with a *zero* and a plus are captured by two built-in class definitions in Haskell...

```
class Monad m => MonadZero m where
   zero :: m a

class MonadZero m => MonadPlus m where
   (++) :: m a -> m a -> m a
```

# Parser Extensions 2(2)

The type constructor Parser can be made instances of these two classes as follows:

• The parser which always fails...

```
instance MonadZero Parser where
zero = Parser (\cs -> [])
```

• The parser which non-deterministically selects...

```
instance MonadPlus Parser where p ++ q = (\cs -> parse p cs ++ parse q cs)
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

41

#### Simple Properties 2(2)

Specifically for the parser monad we can additionally show...

```
zero >>= f = zero
p >>= const zero = zero
    (p ++ q) >>= f = (p >>= f) ++ (q >>= f)
p >>= (\a -> f a ++ g a) = (p >>= f) ++ (p >>= g)
```

Informally:

- ...zero is left-zero and right-zero element for (>>=)
- ...(>>=) distributes through (++)

#### Simple Properties 1(2)

We can show...

```
zero ++ p = p
p ++ zero = p
p ++ (q ++ r) = (p ++ q) ++ r
```

Remark: The above properties are required to hold for each monad with zero and plus

Informally:

- ...zero is left-unit and right-unit for (++)
- ...(++) is associative

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

42

#### **Deterministic Selection**

The parser which deterministically selects...

Note:

- (+++) shows the same behavior as (++), but yields at most one result
- (+++) satisfies all of the previously mentioned properties of (++)

#### **Further Parsers**

Recognizing...

• single objects satisfying a particular property

```
sat :: (Char -> Bool) -> Parser Char
sat p = do {c <- item; if p c then return c else zero}</pre>
```

• single objects

```
char :: Char -> Parser Char
char c = sat (c ==)
```

• sequences of numbers, lower case and upper case characters, etc.

...analogously to char

Compare: sat and char VS. spot and token

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

# Recursion Combinators 1(3)

Useful parsers can often recursively be defined...

Parse a specific string

```
string :: String -> Parser String
string "" = return ""
string (c:cs) = do {char c; string cs; return (c:cs)}
```

• Parse repeated applications of a parser p

```
(Zero or more applications of p)
many :: Parser a -> Parser [a]
many p = many1 p +++ return []

(One or more applications of p)
many1 :: Parser a -> Parser [a]
many1 p = do {a <- p; as <- many p; return (a:as)}</pre>
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

16

# **Recursion Combinators 2(3)**

• Similar to the parser many but with interspersed applications of the parser sep, whose result values are thrown away

# **Recursion Combinators 3(3)**

 Parse repeated applications of a parser p, separated by applications of a parser op, whose result value is an operator that is assumed to associate to the left, and which is used to combine the results from the p parsers

#### **Lexical Combinators**

Suitable combinators allow suppression of a lexical analysis (token recognition), which traditionally precedes parsing...

• Parsing of a string with blanks and line breaks

```
space :: Parser String
space = many (sat isSpace)
```

• Parsing of a token by means of parsers p

```
token :: Parser a -> Parser a
token p = do {a <- p; space; return a}</pre>
```

• Parsing of a symbol token

```
symb :: String -> Parser String
symb cs = token (string cs)
```

• Application of parser p, removal of initial blanks

```
apply :: Parser a -> String -> [(a,String)]
apply p = parse (do {space; p}]
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

40

#### Example: Parsing of Expressions 2(3)

Parsing and evaluating expressions (yielding integer values) using the chainl1 combinator to implement the left-recursive production rules for expr and term...

```
expr :: Parser Int
addop :: Parser (Int -> Int -> Int)
mulop :: Parser (Int -> Int -> Int)

expr = term 'chainl1' addop
term = factor 'chainl1' mulop
factor = digit +++ do {symb "("; n <- expr; symb ")"; return n}
digit = do {x <- token (sat isDIgit); return (ord x - ord '0')}

addop = do {symb "+"; return (+)} +++ do {symb "-"; return (-)}
mulop = do {symb "*"; return (*)} +++ do {symb "/"; return (div)}</pre>
```

#### Example: Parsing of Expressions 1(3)

#### Grammar:

...for arithmetic expressions built up from single digits using the operators +, -, \*, /, and parentheses:

```
expr ::= expr addop term | term
term ::= term mulop factor | factor
factor ::= digit | (expr)
digit ::= 0 | 1 | ... | 9

addop ::= + | -
mulop ::= * | /
```

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

50

# Example: Parsing of Expressions 3(3)

#### Example:

**Evaluating** 

```
apply expr " 1 - 2 * 3 + 4 "
gives the singleton list
```

```
[(-1,"")] as desired as desired.
```

# Further Readings 1(3)

On combinator parsing...

- J. Fokker. Functional Parsers. In: Advanced Functional Programming, First International Summer School, Springer, LNCS 925 (1995), 1-23.
- S. Hill. *Combinators for Parsing Expressions*. Journal of Functional Programming 6:445-463, 1996.
- P. Koopman, R. Plasmeijer. *Efficient Combinator Parsers*. In Proceedings of Implementation of Functional Languages, Springer, LNCS 1595 (1999), 122-138.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

53

55

# Further Readings 3(3)

On parser libraries...

- Daan Leijen, Erik Meijer. *Parsec: A Practical Parser Library*. Electronic Notes in Theoretical Computer Science 41(1), 2001.
- A. Gill, S. Marlow. *Happy The Parser Generator for Haskell*. University of Glasgow, 1995.

http://www.haskell.org/happy

#### Further Readings 2(3)

On error-correcting parsing...

- P. Wadler. How to Replace Failure with a List of Successes, in: Functional Programming Languages and Computer Architectures, Springer, LNCS 201 (1985), 113 128.
- D. Swierstra, P. Azero Alcocer. Fast, Error Correcting Parser Combinators: A Short Tutorial. In Proceedings SOF-SEM'99, Theory and Practice of Informatics, 26th Seminar on Current Trends in Theory and Practice of Informatics, Springer, LNCS 1725 (1999), 111-129.
- D. Swierstra, L. Duponcheel. *Deterministic, Error Correcting Combinator Parsers*. In: *Advanced Functional Programming, Second International Spring School*, Springer, LNCS 1129 (1996), 184-207.

Advanced functional Programming (SS 2010) / Part 6 (Thu, 04/29/10)

54

#### Next Course Meeting...

• Thu, May 6, 2010, lecture time: 4.15 p.m. to 5.45 p.m., lecture room on the ground floor of the building Argentinierstr. 8