## Assignment 4

## **Advanced Functional Programming**

## Thema: Streams

Issued on: 04/24/2009, due date: 05/07/2009

For this assignment a Haskell script named AssFFP4.hs shall be written offering functions which solve the problems described below. This file AssFFP4.hs shall be stored in the home directory of your individual account (not of your group account), as usual on the top most level. Comment your programs meaningfully. Use constants and auxiliary functions, where appropriate.

- Implement a 0-ary Haskell function pof2s :: [Integer], which computes the stream of the powers of 2,i.e., the stream [1,2,4,8,16,32,....
  - Try to implement pof2s recursively using only map, the list constructor : and arithmetic functions.
- The following figure shows the initial part of Pascal's triangle:

We denote the rows of this triangle as P-tuples.

Implement a 0-ary Haskell function pts :: [[Integer]], which gives the stream of P-tuples, i.e. the stream [[1],[1,1],[1,2,1],[1,3,3,1],....

Try to implement pts recursively using only zipWith (together with the standard list constructors and operators and arithmetic operations).

• Let  $n \geq 1$  be a natural number and let  $d_1 d_2 \dots d_k$  be the sequence of decimal numeric characters of n. Moreover, let  $p_1, p_2, p_3, \dots, p_k, \dots$  be the sequence of prime numbers. Then the number

$$2^{d_1}3^{d_2}5^{d_3}\dots p_k^{d_k}$$

is called the  $G\ddot{o}del\ number$  of n. For example,  $144=2^4*3^2$  is the Gödel number of 42 and  $400=2^4*3^0*5^2$  is the Gödel number of 402.

- 1. Write a Haskell function g:: Integer -> Integer, which maps positive arguments to their Gödel number, non-positive arguments to 0.
- 2. Write a 0-ary Haskell function gs:: [Integer], which gives the stream of Gödel numbers starting at 1, i.e. the first element of the stream is the Gödel number of 1, the second element is the Gödel number of 2, etc.

• In honour of Lambert Meerten a positive natural number n, which coincides with its Gödel number, is called a *Meerten number*. A number, which differs at most by d with  $d \in \mathbb{N}_0$  from its Meerten number, we call a d-Meerten number.

Write a Haskell function dM :: Integer -> [Integer], which gives for non-negative arguments d the stream of d-Meerten numbers, for negative arguments the 0-stream, i.e. the stream which consists solely of zeros. Note that for d=0, dM yields the stream of Meerten numbers.

Remark: Meerten numbers are "rare". For d=0 your algorithm might need very much time.