Today's Topic

Parsing: Lexical and syntactical analysis

- Combinator parsing
- Monadic parsing

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Lexical and Syntactical Analysis

• ...in the following summarized as parsing

...an application of functional programming typically used to demonstrate its power and elegance.

Enjoys a long history. An early work for example is...

• W. Burge. *Recursive Programming Techniques*, Addison-Wesley, 1975.

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

2

Parsing – Implementation Variants

Two variants...

- Combinator parsing
 - \rightarrow recursive descent parsing
 - Graham Hutton. Higher-Order Functions for Parsing. Journal of Functional Programming 2(3):323-343, 1992.
- Monadic parsing
 - Graham Hutton, Erik Meijer. Monadic Parser Combinators. Technical Report NOTTCS-TR-96-4, Dept. of Computer Science, University of Nottingham, 1996.

Reference

The following presentation is based on...

- Kapitel 17
 Simon Thompson. Haskell The Craft of Functional Programming, Addison-Wesley, 2nd edition, 1999.
- Graham Hutton, Erik Meijer. *Monadic Parsing in Haskell*. Journal of Functional Programming 1(1), 1993.

Parsing informally

The basic problem...

- Read a sequence of objects of type a and
- extract from this sequence an object or a list of objects of type b.

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

_

Initial Considerations 1(2)

What should be the type of a parsing function?

We have to answer...

How shall the parser behave if there ...

- ...are multiple results?
- ...is a failure?

Example: Parsing of Expressions

Consider...

Expressions

The parsing task to be solved...

• Read an expression of the form ((2+3)*3) and yield the corresponding expression of type expr.

(Note: this can be considered the reverse of the show function. Note also the difference of our function to the derived function read).

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

6

Initial Considerations 2(2)

Now we have to answer...

What shall be done with the remaining input?

Type of the Parser 1(2)

The conclusion of our initial considerations...

```
type Parse a b = [a] \rightarrow [(b,[a])]
-- Parser Input
                        Expected Output
           "(xyz" --> [('(', "xyz")]
bracket
                   --> [(2,"34"), (23,"4"), (234,"")]
number
           "234" --> []
bracket
```

Remark:

• The capability of delivering multiple results enables the analysis of ambiguous grammars

→ list of successes technique

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Basic Parsers 1(3)

• Primitive, input-independent parsing functions

```
-- The always failing parsing function
none :: Parse a b
none inp = []
-- The always successful parsing function
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Remark: The succeed parser does not consume its input. In BNF-notation this corresponds to the symbol ε representing the empty word.

11

Type of the Parser 2(2)

Convention:

- Delivery of the empty list ...signals failure of the analysis.
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component is the input not yet considered.

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

10

Basic Parsers 2(3)

Recognizing single objects (token)...

```
token :: Eq a => a -> Parse a a
token t (x:xs)
  l t. == x
                = \lceil (t.xs) \rceil
  | otherwise = []
token t []
```

• Recognizing single objects satisfying a particular property...

```
spot :: (a -> Bool) -> Parse a a
spot p (x:xs)
  l p x
              = [(x,xs)]
  | otherwise = []
spot p []
```

Basic Parsers 3(3)

Application:

```
bracket = token '('
dig = spot isDigit

isDigit :: Char -> Bool
isDigit ch = ('0' <= ch) && (ch <= '9')

Note: ...token can be defined by means of spot
token t = spot (== t)</pre>
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Combining Parsers 2(4)

• Sequential composition of parsers

Underlying intuition:

...an operator expression starts with a bracket followed by a number

Combining Parsers 1(4)

...to obtain (more) complex parsing functions

→ Combinator Parsing

Alternatives

```
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp
```

Underlying intuition:

...an expression is either a literal, or a variable or an operator expression

Example:

```
(bracket 'alt' dig) "234" --> [] ++ [(2,"34")]
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

14

Combining Parsers 3(4)

Example:

13

Combining Parsers 4(4)

• Transformation/Modification

```
build :: Parse a b -> (b -> c) -> Parse a c
build p f inp = [ (f x, rem) | (x,rem) <- p inp ]

Example:

(digList 'build' digsToNum) "21a3"
    --> [ (digsToNum x,rem) | (x,rem) <- digList "21a3" ]
    --> [ (digsToNum x,rem) | (x,rem) <- [("2","1a3"),("21","a3")]]
    --> [ (digsToNum "2", "1a3"), (digsToNum "21", "a3") ]
    --> [ (2,"1a3"), (21,"a3") ]
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

17

19

Example: Parsing a List of Objects

...supposing we are given a parser recognizing single objects

Intuition:

Note: The combinators alt, >*> and build together with the basic parsers constitute a universal "parser basis".

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

18

Summary and Conclusion

...about combining parsers (parser combinators)

- Parsing functions in the above fashion are structurally similar to grammars in BNF-form. For each operator of the BNF-grammar there is a corresponding (higher-order) parsing function.
- These higher-order functions *combine* simple(r) parsing functions to (more) complex parsing functions.
- They are thus also called *combining forms*, or, as a short hand, *combinators* (cf. Graham Hutton. *Higher-Order Functions for Parsing*).

Overview of the Parsing Functions 1(4)

```
-- Sequence operator
infixr 5 >*>

-- Parser type
type Parse a b = [a] -> [(b,[a])]

-- Input-independent parsing functions
none :: Parse a b
none inp = []

succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Overview of the Parsing Functions 2(4)

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Overview of the Parsing Functions 4(4)

Overview of the Parsing Functions 3(4)

```
-- Alternatives

alt :: Parse a b -> Parse a b -> Parse a b

alt p1 p2 inp = p1 inp ++ p2 inp

-- Sequences
(>*>) :: Parse a b -> Parse a c -> Parse a (b,c)
(>*>) p1 p2 inp

= [((y,z),rem2) | (y,rem1) <- p1 inp, (z,rem2) <- p2 rem1]

-- Transformation/Modification
build :: Parse a b -> (b -> c) -> Parse a c
build pf inp = [ (f x, rem) | (x,rem) <- p inp]
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

22

Application: Back to the initial Example

We consider expressions of the form...

```
data Expr = Lit Int | Var Name | Op Ops Expr Expr
data Ops = Add | Sub | Mul | Div | Mod

Op Add (Lit 2) (Lit 3) corresponds to 2+3
```

...where the following convention shall hold:

- \bullet *Literals* ...67, \sim 89, etc., where \sim is used for unary minus
- Names ...the lower case characters from 'a' to 'z'
- Applications of the binary operations ...+,*,-,/,%, where
 is used for mod and / for integer division.

A Parser for Expressions 1(3)

The parser consists...

```
parser :: Parse Char Expr
parser = litParse 'alt' nameParse 'alt' opExpParse
```

... of three parts corresponding to the three sorts of expressions.

Parsing names of variables...

```
nameParse :: Parse Char Expr
nameParse = spot isName 'build' Name
isName :: Char -> Bool
isName x = ('a' <= x && x <= 'z')</pre>
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

25

A Parser for Expressions 3(3)

Note that a number of supporting functions used such as...

- isOp
- $\bullet \ \, charlistToExpr$
- ...

are yet to be defined.

A Parser for Expressions 2(3)

Parsing (fully bracketed binary) operator expressions...

```
opExpParse
  = (token '(' >*>
      parser >*>
      spot isOp >*>
      parser >*>
      token ')')
      'build' makeExpr

Parsing literals (numerals)...

litParse
  = ((optional (token '~')) >*>
      (neList (spot isDigit))
      'build' (charlistToExpr . uncurry (++))
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

26

The Top-level Parser

Converting a string to the expression it represents...

Note: The input string is provided by the value of inp.

Summary and Conclusion 1(2)

Parser of the form...

```
type Parse a b = [a] -> [(b,[a])]

none :: Parse a b
succeed :: b -> Parse a b
spot :: (a -> Bool) -> Parse a a
alt :: Parse a b -> Parse a b -> Parse a b
>*> :: Parse a b -> Parse a c -> Parse a (b,c)
build :: Parse a b -> (b -> c) -> Parse a c
topLevel :: Parse a b -> [a] -> b
```

...support particularly well the construction of so-called *recursive descent* parsers.

29

31

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Monadic Parsing

```
newtype Parser a = Parser (String -> [(a,String)])
```

We use again the convention:

- Delivery of the empty list ...signals failure of the analysis
- Delivery of the non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component the input still to be considered

Summary and Conclusion 2(2)

The followoing language features proved invaluable...

- Higher-order functions ...Parse a b is of a functional type; all parser combinators are thus higher-order functions, too.
- Polymorphism ...consider again the type of Parse a b: the above parser combinator can immediately be reused for other (token-) and data types.
- Lazy evaluation ... "on demand" generation of the possible parses, automatical backtracking.

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

30

Basic Parsers

• Recognizing single characters...

Compare: item VS. token

The Parser Monad

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Compare: return vs. succeed and (>>=) vs. infixr

33

Typical Structure of a Parser 1(2)

```
...using the operator (>>=)
```

```
p1 >>= \a1 ->
p2 >>= \a2 ->
...
pn >>= \an ->
f a1 a2 ... an
```

Intuition:

- Apply parser p1 and denote its result a1
- Apply subsequently parser p2 and denote its result a2
- ..
- Apply concludingly parser pn and denote its result an
- Combine finally the intermediate results by applying some suitable function f

Properties of return and (>>=)

As required for instances of class Monad, we can show...

```
return a >>= f = f a

p >>= return = p

p >>= (\a -> (f a >>= g)) = (p >>= (\a -> f a)) >>= g
```

Reminder:

- The above properties are required for each instance of class Monad, not just for the specific instance of the parser monad
 - ...return is left-unit and right-unit for (>>=)
 → ...allows a simpler and more concise definition of some parsers
 - ...(>>=) is associative
 - → ...allows suppression of parentheses when parsers are applied sequentially

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

34

Typical Structure of a Parser 2(2)

The do-notation allows a more elegant notation...

```
do a1 <- p1
  a2 <- p2
  ...
  an <- pn
  f a1 a2 ... an</pre>
```

Alternatively, in just one line...

```
do {a1 <- p1; a2 <- p2; ...; an <- pn; f a1 a2 ... an}
```

Notational Conventions

Expressions of the form

• ai <- pi are called *generators* (since they generate values for the variables ai)

Remark:

A generator of the form ai <- pi can be

• replaced by pi, if the generated value will not be used afterwards

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

37

Examples

```
p :: Parser (Char,Char)
p = do {c <- item; item; d <- item; return (c,d)}</pre>
```

Informally: Parser p...

- reads three characters
- drops the second character of these and
- returns the first and the third character as a pair

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

38

Parser Extensions 1(2)

Monad with zero and plus...

```
class Monad m => MonadZero m where
   zero :: m a

class MonadZero m => MonadPlus m where
   (++) :: m a -> m a -> m a
```

Parser Extensions 2(2)

The parser which always fails...

```
instance MonadZero Parser where
zero = Parser (\cs -> [])
```

The parser which non-deterministically selects...

```
instance MonadPlus Parser where
p ++ q = (\cs -> parse p cs ++ parse q cs)
```

Simple Properties 1(2)

We can show...

```
zero ++ p = p
p ++ zero = p
p ++ (q ++ r) = (p ++ q) ++ r
```

Remark: The above properties are required to hold for each monad with zero and plus

Informally:

- ...zero is left-unit and right-unit for (++)
- ...(++) is associative

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

11

Deterministic Selection

The parser which deterministically selects...

```
(+++) :: Parser a -> Parser a -> Parser a
p +++ q = Parser (\cs -> case parse (p ++ q) cs of
[] -> []
(x:xs) -> [x])
```

Note:

- (+++) shows the same behavior as (++), but yields at most one result
- (+++) satisfies all of the previously mentioned properties of (++)

Simple Properties 2(2)

Specifically for the parser monad we can show...

```
zero >>= f = zero
p >>= const zero = zero
    (p ++ q) >>= f = (p >>= f) ++ (q >>= f)
p >>= (\a -> f a ++ g a) = (p >>= f) ++ (p >>= g)
```

Informally:

- ...zero is left-zero and right-zero element for (>>=)
- ...(>>=) distributes through (++)

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

42

Further Parsers

Recognizing...

• single objects satisfying a particular property

```
sat :: (Char -> Bool) -> Parser Char
sat p = do {c <- item; if p c then return c else zero}</pre>
```

• single objects

```
char :: Char -> Parser Char
char c = sat (c ==)
```

• sequences of numbers, lower case and upper case characters, etc.

...analogously to char

Compare: sat and char vs. spot and token

Recursion Combinators 1(3)

Parsers can often recursively be defined...

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

45

Recursion Combinators 3(3)

```
-- Parse repeated applications of a parser p, separated by
-- applications of a parser op, whose result value is an operator
-- that is assumed to associate to the left, and which is used
-- to combine the results from the p parsers

chainl :: Parser a -> Parser (a -> a -> a) -> a -> Parser a
chainl p op a = (p 'chainl1' op) +++ return a

chainl1 :: Parser a -> Parser (a -> a -> a) -> Parser a
p 'chainl1' op = do {a <- p; rest a}

where

rest a = (do f <- op
b <- p
rest (f a b))
+++ return a
```

Recursion Combinators 2(3)

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

46

Lexical Combinators

Suitable combinators allow suppression of a lexical analysis (token recognition)...

```
-- Parsing of a string with blanks and line breaks space :: Parser String space = many (sat isSpace)

-- Parsing of a token by means of parsers p token :: Parser a -> Parser a token p = do {a <- p; space; return a}

-- Parsing of a symbol token symb :: String -> Parser String symb cs = token (string cs)

-- Application of parser p, removal of initial blanks apply :: Parser a -> String -> [(a,String)] apply p = parse (do {space; p}]
```

Example: Parsing of Expressions 1(3)

Grammar:

```
expr ::= expr addop term | term
term ::= term mulop factor | factor
factor ::= digit | (expr)
digit ::= 0 | 1 | ... | 9

addop ::= + | -
mulop ::= * | /
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

Example: Parsing of Expressions 3(3)

Example:

```
apply expr " 1 - 2 * 3 + 4 "

--> [(-1,"")] as desired
```

Example: Parsing of Expressions 2(3)

Parsing and evaluating expressions (yielding integer values)...

```
expr :: Parser Int
addop :: Parser (Int -> Int -> Int)
mulop :: Parser (Int -> Int -> Int)

expr = term 'chainl1' addop
term = factor 'chainl1' mulop
factor = digit +++ do {symb "("; n <- expr; symb ")"; return n}
digit = do {x <- token (sat isDIgit); return (ord x - ord '0')}

addop = do {symb "+"; return (+)} +++ do {symb "-"; return (-)}
mulop = do {symb "*"; return (*)} +++ do {symb "/"; return (div)}</pre>
```

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

50

Further Readings 1(3)

On combinator parsing...

- J. Fokker. Functional Parsers. In: Advanced Functional Programming, First International Summer School, Springer, LNCS 925 (1995), 1-23.
- S. Hill. *Combinators for Parsing Expressions*. Journal of Functional Programming 6:445-463, 1996.
- P. Koopman, R. Plasmeijer. Efficient Combinator Parsers.
 In Proceedings of Implementation of Functional Languages, Springer, LNCS 1595 (1999), 122-138.

Further Readings 2(3)

On error-correcting parsing...

- P. Wadler. How to Replace Failure with a List of Successes, in: Functional Programming Languages and Computer Architectures, Springer, LNCS 201 (1985), 113 128.
- D. Swierstra, P. Azero Alcocer. Fast, Error Correcting Parser Combinators: A Short Tutorial. In Proceedings SOF-SEM'99, Theory and Practice of Informatics, 26th Seminar on Current Trends in Theory and Practice of Informatics, Springer, LNCS 1725 (1999), 111-129.
- D. Swierstra, L. Duponcheel. *Deterministic, Error Correcting Combinator Parsers*. In: *Advanced Functional Programming, Second International Spring School*, Springer, LNCS 1129 (1996), 184-207.

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

53

Next lecture...

 Thu, June 21, 2007, lecture time: 4.15 p.m. to 5.45 p.m., lecture room on the ground floor of the building Argentinierstr. 8

Sixth (final) assignment (as well as previous assignments)...

• Please check out the homepage of the course for details.

Further Readings 3(3)

On parser libraries...

- Daan Leijen, Erik Meijer. *Parsec: A Practical Parser Library*. Electronic Notes in Theoretical Computer Science 41(1), 2001.
- A. Gill, S. Marlow. *Happy The Parser Generator for Haskell*. University of Glasgow, 1995.

http://www.haskell.org/happy

Advanced functional Programming (SS 2007) / Part 7 (Thu, 06/14/07)

54