Today's Topic

Parsing: Lexical and syntactical analysis

- Combinator parsing
- Monadic parsing

Lexical and Syntactical Analysis

• ...in the following summarized as parsing

...an application of functional programming typically used to demonstrate its power and elegance.

Enjoys a long history. An early work for example is...

• W. Burge. *Recursive Programming Techniques*, Addison-Wesley, 1975.

Parsing – Implementation Variants

Two variants...

- Combinator parsing

 - Graham Hutton. Higher-Order Functions for Parsing. Journal of Functional Programming 2(3):323-343, 1992.
- Monadic parsing
 - Graham Hutton, Erik Meijer. Monadic Parser Combinators. Technical Report NOTTCS-TR-96-4, Dept. of Computer Science, University of Nottingham, 1996.

Reference

The following presentation is based on...

- Kapitel 17
 Simon Thompson. Haskell The Craft of Functional Programming, Addison-Wesley, 2nd edition, 1999.
- Graham Hutton, Erik Meijer. *Monadic Parsing in Haskell*. Journal of Functional Programming 1(1), 1993.

Parsing informally

The basic problem...

- Read a sequence of objects of type a and
- extract from this sequence an object or a list of objects of type b.

Example: Parsing of Expressions

Consider...

Expressions

The parsing task to be solved...

 Read an expression of the form ((2+3)*3) and yield the corresponding expression of type expr.

(Note: this can be considered the reverse of the show function. Note also the difference of our function to the derived function read).

Initial Considerations 1(2)

What should be the type of a parsing function?

We have to answer...

How shall the parser behave if there ...

- ...are multiple results?
- ...is a failure?

Initial Considerations 2(2)

Now we have to answer...

What shall be done with the remaining input?

Type of the Parser 1(2)

The conclusion of our initial considerations...

Remark:

• The capability of delivering multiple results enables the analysis of ambiguous grammars

→ list of successes technique

Type of the Parser 2(2)

Convention:

- Delivery of the empty list ... signals failure of the analysis.
- Delivery of a non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component is the input not yet considered.

Basic Parsers 1(3)

Primitive, input-independent parsing functions

```
-- The always failing parsing function
none :: Parse a b
none inp = []

-- The always successful parsing function
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Remark: The succeed parser does not consume its input. In BNF-notation this corresponds to the symbol ε representing the empty word.

Basic Parsers 2(3)

• Recognizing single objects (token)...

Recognizing single objects satisfying a particular property...

Basic Parsers 3(3)

```
Application:
```

```
bracket = token '('
dig = spot isDigit

isDigit :: Char -> Bool
isDigit ch = ('0' <= ch) && (ch <= '9')

Note: ...token can be defined by means of spot
token t = spot (== t)</pre>
```

Combining Parsers 1(4)

...to obtain (more) complex parsing functions \sim Combinator Parsing

Alternatives

```
alt :: Parse a b -> Parse a b -> Parse a b alt p1 p2 inp = p1 inp ++ p2 inp
```

Underlying intuition:

...an expression is either a literal, or a variable or an operator expression

Example:

```
(bracket 'alt' dig) "234" --> [] ++ [(2, "34")]
```

Combining Parsers 2(4)

Sequential composition of parsers

Underlying intuition:

...an operator expression starts with a bracket followed by a number

Combining Parsers 3(4)

Example:

```
Because of number "24(" --> [(2, "4("), (24, "("))] we obtain
(number >*> bracket) "24("
   --> [((y,z),rem2) | (y,rem1) < - [(2,"4("), (24,"(")],
                        (z.rem2) <- bracket rem1 ]
   --> [((2,z),rem2) | (z,rem2) < -bracket "4("] ++
        [((24,z),rem2) | (z,rem2) <- bracket "("]
   --> [] ++ [((24,z),rem2) | (z,rem2) <- bracket "("]
Because of "(" --> [('(',"")] we obtain finally
   --> [((24,z),rem2) | (z,rem2) < - [('(',"")]]
   --> [ ((24,'('), "") ]
```

Combining Parsers 4(4)

• Transformation/Modification

Example: Parsing a List of Objects

...supposing we are given a parser recognizing single objects

Intuition:

- A list can be empty.
- A list can be non-empty.
 - → ...recognized by the combined parser p >*> list p

Note: The combinators alt, >*> and build together with the basic parsers constitute a universal "parser basis".

Summary and Conclusion

...about combining parsers (parser combinators)

- Parsing functions in the above fashion are structurally similar to grammars in BNF-form. For each operator of the BNF-grammar there is a corresponding (higher-order) parsing function.
- These higher-order functions *combine* simple(r) parsing functions to (more) complex parsing functions.
- They are thus also called *combining forms*, or, as a short hand, *combinators* (cf. Graham Hutton. *Higher-Order Functions for Parsing*).

Overview of the Parsing Functions 1(4)

```
-- Sequence operator
infixr 5 > *>
-- Parser type
type Parse a b = [a] \rightarrow [(b,[a])]
-- Input-independent parsing functions
none :: Parse a b
none inp = []
succeed :: b -> Parse a b
succeed val inp = [(val,inp)]
```

Overview of the Parsing Functions 2(4)

Overview of the Parsing Functions 3(4)

```
-- Alternatives
alt :: Parse a b -> Parse a b -> Parse a b
alt p1 p2 inp = p1 inp ++ p2 inp
-- Sequences
(>*>) :: Parse a b -> Parse a c -> Parse a (b,c)
(>*>) p1 p2 inp
 = [((y,z),rem2) | (y,rem1) <- p1 inp, (z,rem2) <- p2 rem1]
-- Transformation/Modification
build :: Parse a b -> (b -> c) -> Parse a c
build p f inp = [(f x, rem) | (x, rem) < - p inp]
```

Overview of the Parsing Functions 4(4)

Application: Back to the initial Example

We consider expressions of the form...

```
data Expr = Lit Int | Var Name | Op Ops Expr Expr
data Ops = Add | Sub | Mul | Div | Mod
Op Add (Lit 2) (Lit 3) corresponds to 2+3
```

...where the following convention shall hold:

- Literals ...67, \sim 89, etc., where \sim is used for unary minus
- Names ...the lower case characters from 'a' to 'z'
- Applications of the binary operations ...+,*,-,/,%, where % is used for mod and / for integer division.

A Parser for Expressions 1(3)

The parser consists...

```
parser :: Parse Char Expr
parser = litParse 'alt' nameParse 'alt' opExpParse
```

...of three parts corresponding to the three sorts of expressions.

Parsing names of variables...

```
nameParse :: Parse Char Expr
nameParse = spot isName 'build' Name
isName :: Char -> Bool
isName x = ('a' <= x && x <= 'z')</pre>
```

A Parser for Expressions 2(3)

Parsing (fully bracketed binary) operator expressions...

```
opExpParse
    = (token '(' >*>
       parser
                 >*>
       spot isOp >*>
       parser
               >*>
       token ')')
       'build' makeExpr
Parsing literals (numerals)...
  litParse
   = ((optional (token '~')) >*>
       (neList (spot isDigit))
      'build' (charlistToExpr . uncurry (++))
```

A Parser for Expressions 3(3)

Note that a number of supporting functions used such as...

- isOp
- charlistToExpr
- ...

are yet to be defined.

The Top-level Parser

Converting a string to the expression it represents...

Note: The input string is provided by the value of inp.

Summary and Conclusion 1(2)

Parser of the form...

```
type Parse a b = [a] -> [(b,[a])]

none :: Parse a b
succeed :: b -> Parse a b
spot :: (a -> Bool) -> Parse a a
alt :: Parse a b -> Parse a b -> Parse a b
>*> :: Parse a b -> Parse a c -> Parse a (b,c)
build :: Parse a b -> (b -> c) -> Parse a c
topLevel :: Parse a b -> [a] -> b
```

...support particularly well the construction of so-called *recursive descent* parsers.

Summary and Conclusion 2(2)

The followoing language features proved invaluable...

- Higher-order functions ...Parse a b is of a functional type; all parser combinators are thus higher-order functions, too.
- Polymorphism ...consider again the type of Parse a b: the above parser combinator can immediately be reused for other (token-) and data types.
- Lazy evaluation ... "on demand" generation of the possible parses, automatical backtracking.

Monadic Parsing

```
newtype Parser a = Parser (String -> [(a,String)])
```

We use again the convention:

- Delivery of the empty list ...signals failure of the analysis
- Delivery of the non-empty list ...signals success of the analysis; each element of the list is a pair, whose first component is the identified object (token) and whose second component the input still to be considered

Basic Parsers

• Recognizing single characters...

Compare: item VS. token

The Parser Monad

Reminder: The class monad class Monad m where return :: a -> m a (>>=) :: m a -> (a -> m b) -> m b Note: Parser is a type constructor. This allows... instance Monad Parser where -- The always successful parser return a = Parser (\cs -> [(a,cs)]) -- Sequences p >>= f = Parser (\cs -> concat [parse (f a) cs' | (a,cs') <- parse p cs]) Compare: return vs. succeed and (>>=) vs. infixr

Properties of return and (>>=)

As required for instances of class Monad, we can show...

Reminder:

- The above properties are required for each instance of class Monad, not just for the specific instance of the parser monad
 - ...return is left-unit and right-unit for (>>=)
 → ...allows a simpler and more concise definition of some parsers
 - ...(>>=) is associative
 - ...allows suppression of parentheses when parsers are applied sequentially

Typical Structure of a Parser 1(2)

...using the operator (>>=)
p1 >>= \a1 ->
p2 >>= \a2 ->
...
pn >>= \an ->
f a1 a2 ... an

Intuition:

- Apply parser p1 and denote its result a1
- Apply subsequently parser p2 and denote its result a2
- ...
- Apply concludingly parser pn and denote its result an
- Combine finally the intermediate results by applying some suitable function f

Typical Structure of a Parser 2(2)

The do-notation allows a more elegant notation...

```
do a1 <- p1
  a2 <- p2
  ...
  an <- pn
  f a1 a2 ... an</pre>
```

Alternatively, in just one line...

```
do {a1 <- p1; a2 <- p2; ...; an <- pn; f a1 a2 ... an}
```

Notational Conventions

Expressions of the form

• ai <- pi are called *generators* (since they generate values for the variables ai)

Remark:

A generator of the form ai <- pi can be

 replaced by pi, if the generated value will not be used afterwards

Examples

```
p :: Parser (Char, Char)
p = do {c <- item; item; d <- item; return (c,d)}</pre>
```

Informally: Parser p...

- reads three characters
- drops the second character of these and
- returns the first and the third character as a pair

Parser Extensions 1(2)

```
Monad with zero and plus...

class Monad m => MonadZero m where
   zero :: m a

class MonadZero m => MonadPlus m where
   (++) :: m a -> m a -> m a
```

Parser Extensions 2(2)

The parser which always fails...

```
instance MonadZero Parser where
zero = Parser (\cs -> [])
```

The parser which non-deterministically selects...

```
instance MonadPlus Parser where
   p ++ q = (\cs -> parse p cs ++ parse q cs)
```

Simple Properties 1(2)

We can show...

$$zero ++ p = p$$

 $p ++ zero = p$
 $p ++ (q ++ r) = (p ++ q) ++ r$

Remark: The above properties are required to hold for each monad with zero and plus

Informally:

- ...zero is left-unit and right-unit for (++)
- ...(++) is associative

Simple Properties 2(2)

Specifically for the parser monad we can show...

Informally:

- ...zero is left-zero and right-zero element for (>>=)
- ...(>>=) distributes through (++)

Deterministic Selection

The parser which deterministically selects...

Note:

- (+++) shows the same behavior as (++), but yields at most one result
- (+++) satisfies all of the previously mentioned properties of (++)

Further Parsers

Recognizing...

single objects satisfying a particular property

```
sat :: (Char -> Bool) -> Parser Char
sat p = do {c <- item; if p c then return c else zero}</pre>
```

• single objects

```
char :: Char -> Parser Char
char c = sat (c ==)
```

sequences of numbers, lower case and upper case characters, etc.

...analogously to char

Compare: sat and char VS. spot and token

Recursion Combinators 1(3)

Parsers can often recursively be defined...

```
-- Parsing of a string
string :: String -> Parser String
string "" = return ""
string (c:cs) = do {char c; string cs; return (c:cs)}

-- Parse repeated applications of a parser p
many :: Parser a -> Parser [a] -- zero or more applications of p
many p = many1 p +++ return []

many1 :: Parser a -> Parser [a] -- one or more applications of p
many1 p = do {a <- p; as <- many p; return (a:as)}</pre>
```

Recursion Combinators 2(3)

Recursion Combinators 3(3)

```
-- Parse repeated applications of a parser p, separated by
-- applications of a parser op, whose result value is an operator
-- that is assumed to associate to the left, and which is used
-- to combine the results from the p parsers
chainl :: Parser a -> Parser (a -> a -> a) -> a -> Parser a
chainl p op a = (p 'chainl1' op) +++ return a
chainl1 :: Parser a -> Parser (a -> a -> a) -> Parser a
p 'chainl1' op = do {a <- p; rest a}</pre>
                 where
                    rest a = (do f <- op
                                 b <- p
                                 rest (f a b))
                             +++ return a
```

Lexical Combinators

Suitable combinators allow suppression of a lexical analysis (token recognition)...

```
-- Parsing of a string with blanks and line breaks
space :: Parser String
space = many (sat isSpace)
-- Parsing of a token by means of parsers p
token :: Parser a → Parser a
token p = do {a <- p; space; return a}
-- Parsing of a symbol token
symb :: String -> Parser String
symb cs = token (string cs)
-- Application of parser p, removal of initial blanks
apply :: Parser a -> String -> [(a,String)]
apply p = parse (do {space; p}]
```

Example: Parsing of Expressions 1(3)

Grammar:

```
expr ::= expr addop term | term
term ::= term mulop factor | factor
factor ::= digit | (expr)
digit ::= 0 | 1 | ... | 9

addop ::= + | -
mulop ::= * | /
```

Example: Parsing of Expressions 2(3)

Parsing and evaluating expressions (yielding integer values)...

```
expr :: Parser Int
addop :: Parser (Int -> Int -> Int)
mulop :: Parser (Int -> Int -> Int)

expr = term 'chainl1' addop
term = factor 'chainl1' mulop
factor = digit +++ do {symb "("; n <- expr; symb ")"; return n}
digit = do {x <- token (sat isDIgit); return (ord x - ord '0')}

addop = do {symb "+"; return (+)} +++ do {symb "-"; return (-)}
mulop = do {symb "*"; return (*)} +++ do {symb "/"; return (div)}</pre>
```

Example: Parsing of Expressions 3(3)

Example:

```
apply expr " 1 - 2 * 3 + 4 " \longrightarrow [(-1,"")] as desired
```

Further Readings 1(3)

On combinator parsing...

- J. Fokker. Functional Parsers. In: Advanced Functional Programming, First International Summer School, Springer, LNCS 925 (1995), 1-23.
- S. Hill. *Combinators for Parsing Expressions*. Journal of Functional Programming 6:445-463, 1996.
- P. Koopman, R. Plasmeijer. *Efficient Combinator Parsers*. In Proceedings of Implementation of Functional Languages, Springer, LNCS 1595 (1999), 122-138.

Further Readings 2(3)

On error-correcting parsing...

- P. Wadler. How to Replace Failure with a List of Successes, in: Functional Programming Languages and Computer Architectures, Springer, LNCS 201 (1985), 113 128.
- D. Swierstra, P. Azero Alcocer. Fast, Error Correcting Parser Combinators: A Short Tutorial. In Proceedings SOF-SEM'99, Theory and Practice of Informatics, 26th Seminar on Current Trends in Theory and Practice of Informatics, Springer, LNCS 1725 (1999), 111-129.
- D. Swierstra, L. Duponcheel. *Deterministic, Error Correcting Combinator Parsers*. In: *Advanced Functional Programming, Second International Spring School*, Springer, LNCS 1129 (1996), 184-207.

Further Readings 3(3)

On parser libraries...

- Daan Leijen, Erik Meijer. *Parsec: A Practical Parser Library*. Electronic Notes in Theoretical Computer Science 41(1), 2001.
- A. Gill, S. Marlow. *Happy The Parser Generator for Haskell*. University of Glasgow, 1995.

http://www.haskell.org/happy

Next lecture...

• Thu, June 21, 2007, lecture time: 4.15 p.m. to 5.45 p.m., lecture room on the ground floor of the building Argentinierstr. 8

Sixth (final) assignment (as well as previous assignments)...

• Please check out the homepage of the course for details.